

High-precision mass measurements for nuclear
structure and fundamental studies ...
... and more

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Content



- Motivation and history
- Experimental setup and measurement procedure
- High-precision mass measurements
- High-precision g-factor measurements
- Summary

The Helmholtz-Research-Group MATS



„Mass“-Team

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C. Haberkorn (ass.), S. Kreim (PhD), C. Rodegheri (PhD),
S. Sturm (PhD), B. Schabinger (PhD), S. Ulmer (PhD)

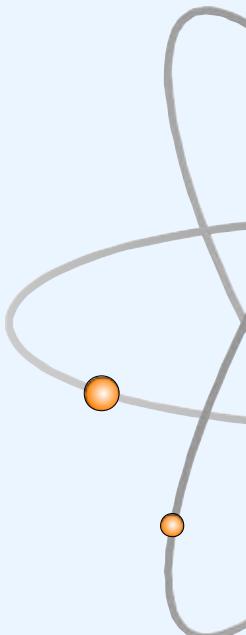
„g-Factor“-Team

In collaboration with:
H.-J. Kluge, H. Kracke, M. Kretzschmar, W. Quint, L. Schweikhard, S. Stahl, J. Walz, G. Werth
and the ISOLTRAP team

High-precision mass measurements

Requirements for mass spectrometry

High-accuracy mass measurements allow one to determine the atomic and nuclear binding energies reflecting all forces in the atom/nucleus.

 $B(Z, N)$

K. B., Phys. Rep. 425, 1-78 (2006)	$\delta m/m$
General physics & chemistry	$\leq 10^{-5}$
Nuclear structure physics - separation of isobars	$\leq 10^{-6}$
Astrophysics - separation of isomers	$\leq 10^{-6}$
Weak interaction studies	$\leq 10^{-8}$
Metrology - fundamental constants	$\leq 10^{-9}$
CPT tests	$\leq 10^{-10}$
QED in highly-charged ions - separation of atomic states	$\leq 10^{-11}$

 $Z \cdot c^2$

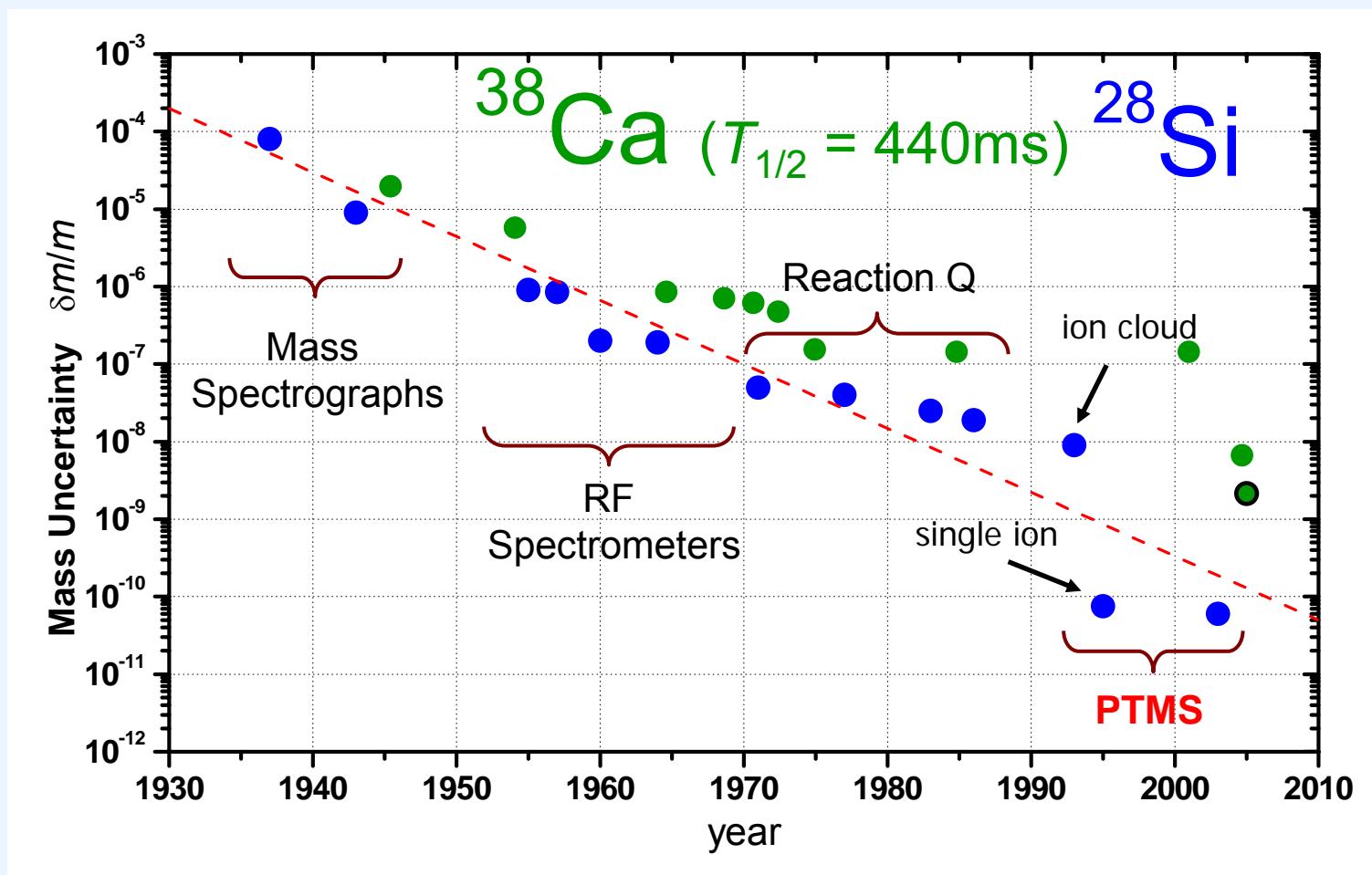
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Precision: A brief history of mass spectrometry

M
A
T
S



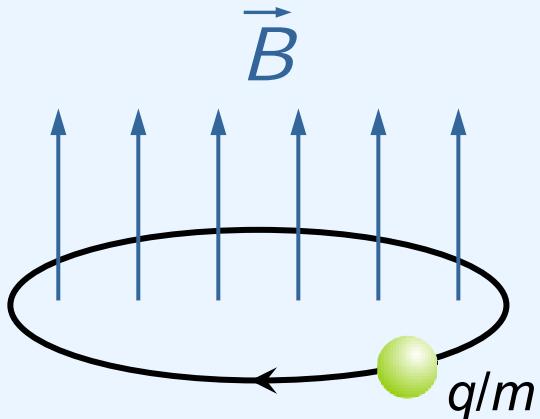
$$m(^{28}\text{Si}) = 27.976\ 926\ 532\ 6 \text{ u}$$

$$\delta m = 0.000\ 000\ 001\ 9 \text{ u}$$

$$\text{Rel. Precision} = 6 \times 10^{-11}$$

Distance Mainz-Trento
800km ± 0.05mm

Principle of Penning trap mass spectrometry

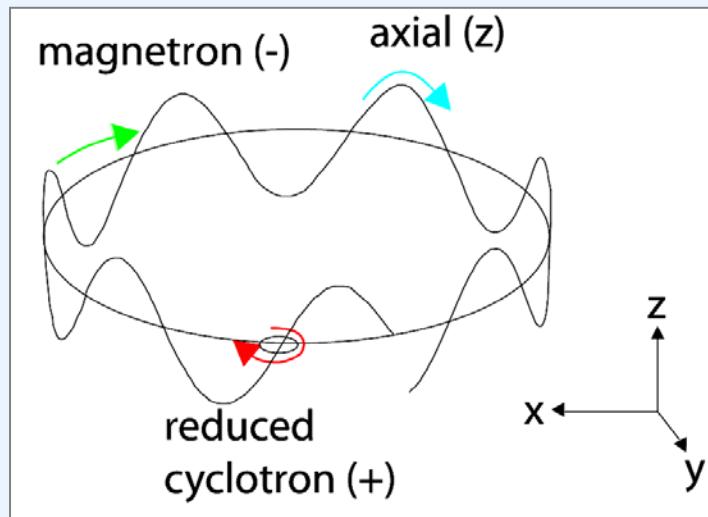
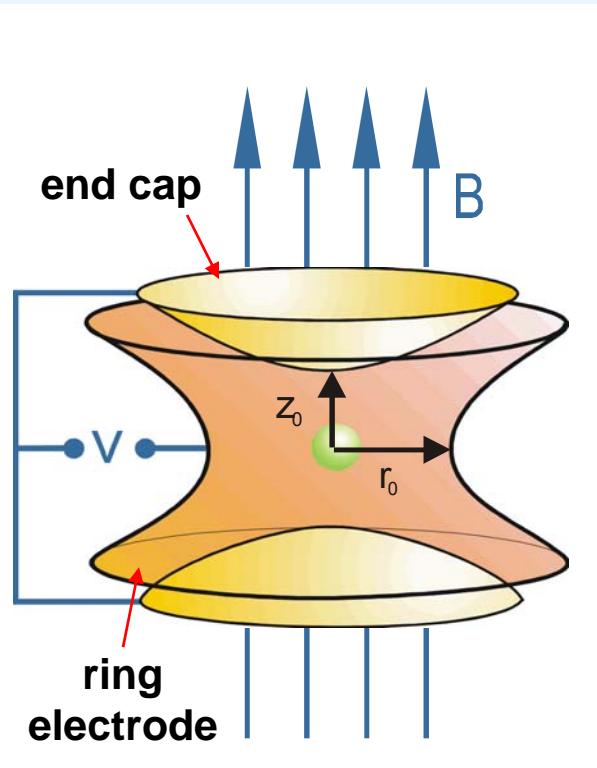


Cyclotron frequency:

$$f_c = \frac{1}{2\pi} \cdot \frac{q}{m} \cdot B$$

PENNING trap

- Strong homogeneous magnetic field
- Weak electric 3D quadrupole field

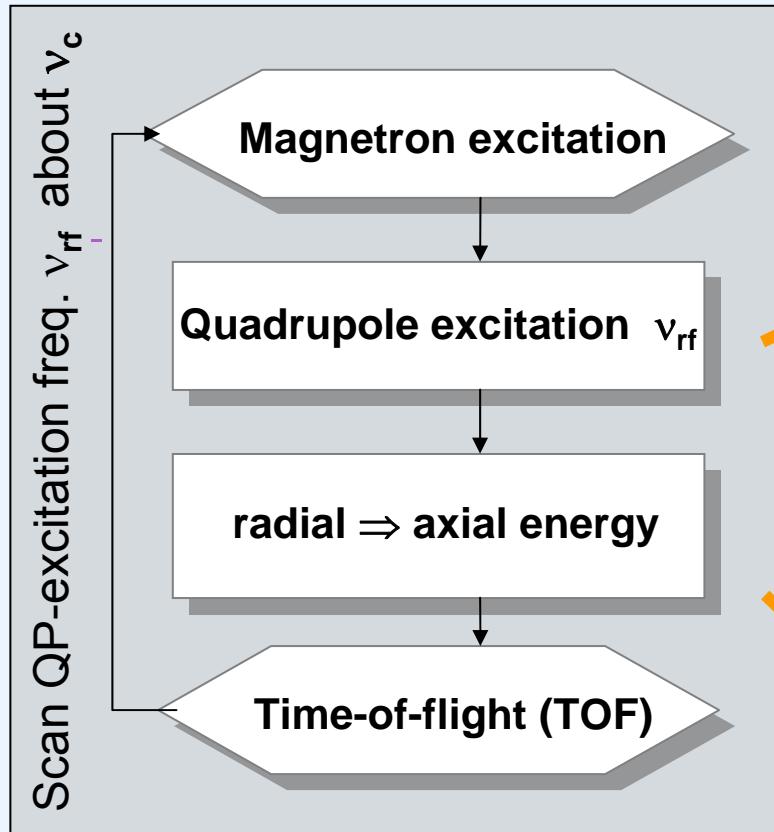


Typical frequencies
 $q = e, m = 100 \text{ u}, B = 6 \text{ T}$
 $\Rightarrow f_- \approx 1 \text{ kHz}$
 $f_+ \approx 1 \text{ MHz}$

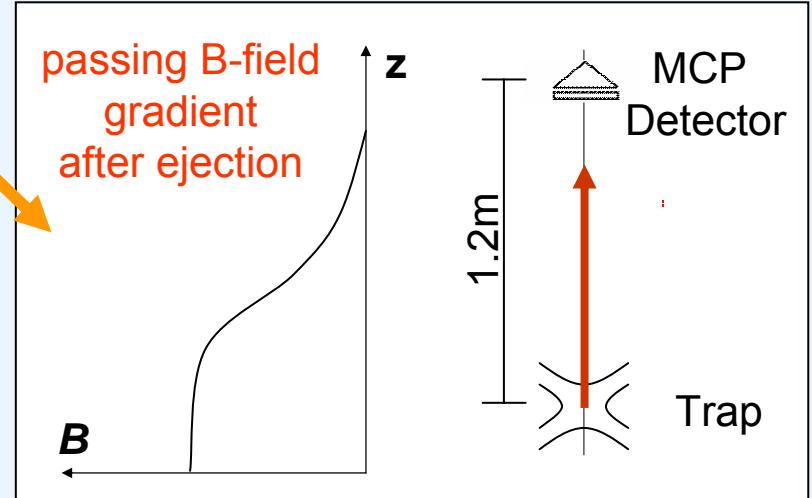
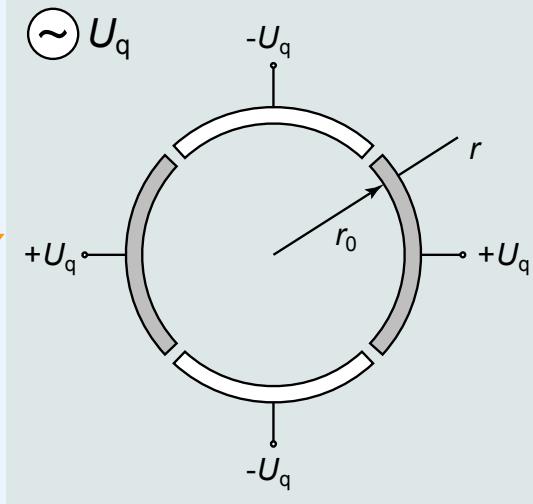
Brown & Gabrielse, Rev. Mod. Phys. 58, 233 (1986)

Time-of-flight mass spectrometry

Time-of-flight resonance technique



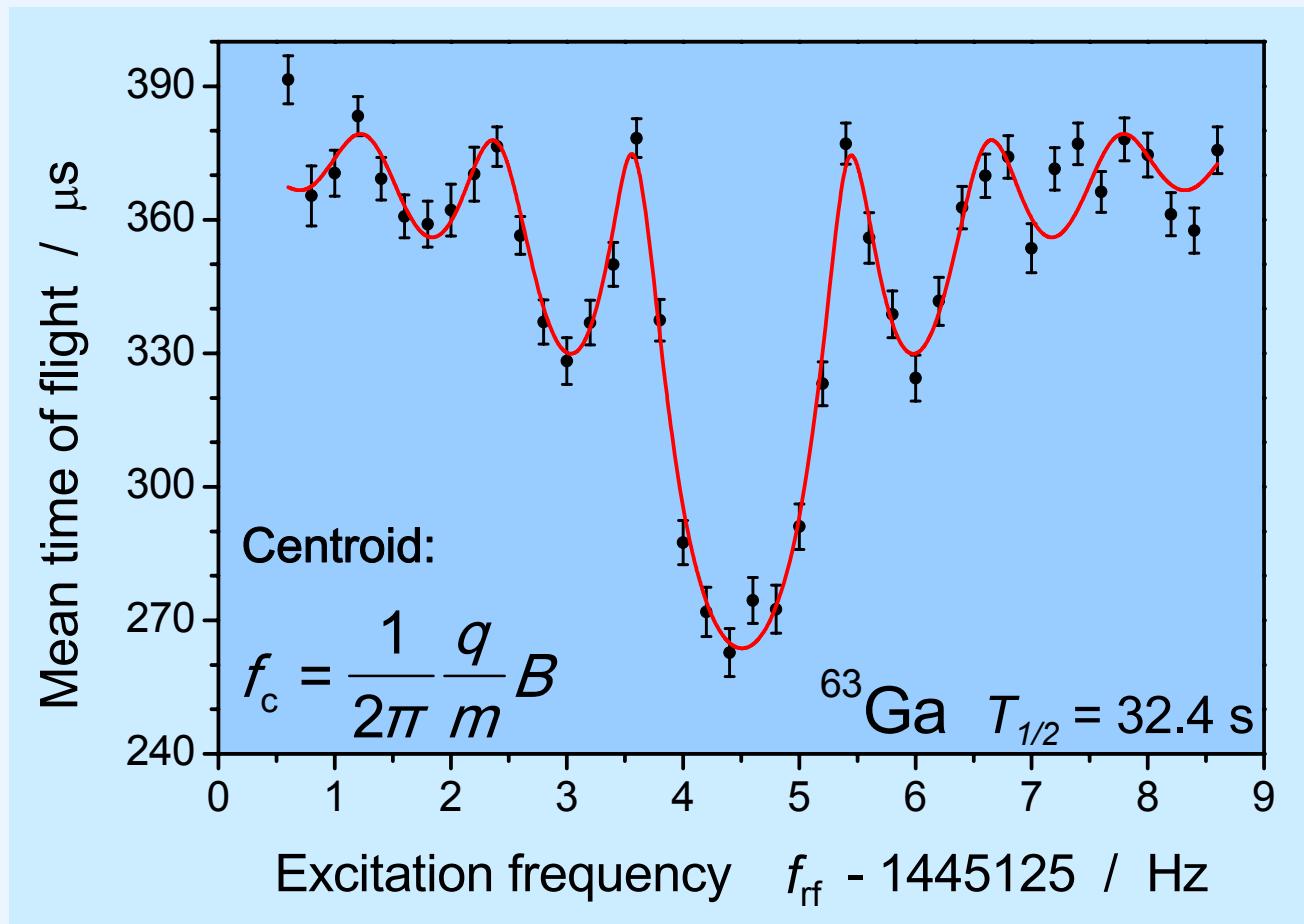
Conversion of magnetron
into cyclotron motion



Resolving power: $R = f_{\text{exc}} T_{\text{exc}}$

TOF cyclotron resonance curve

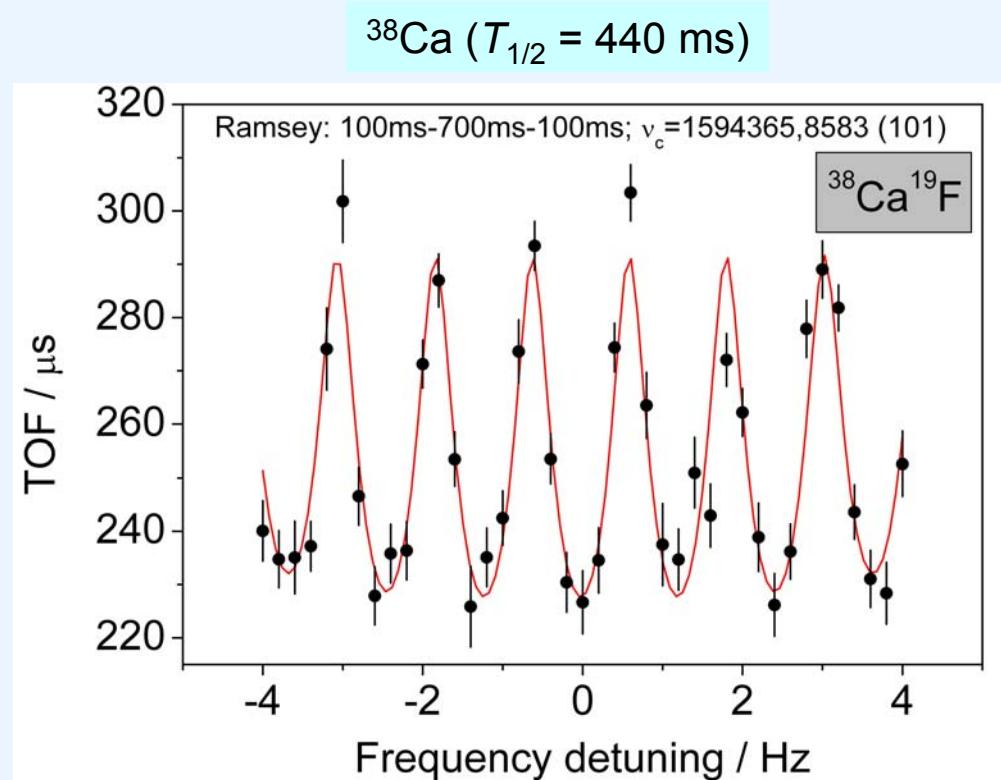
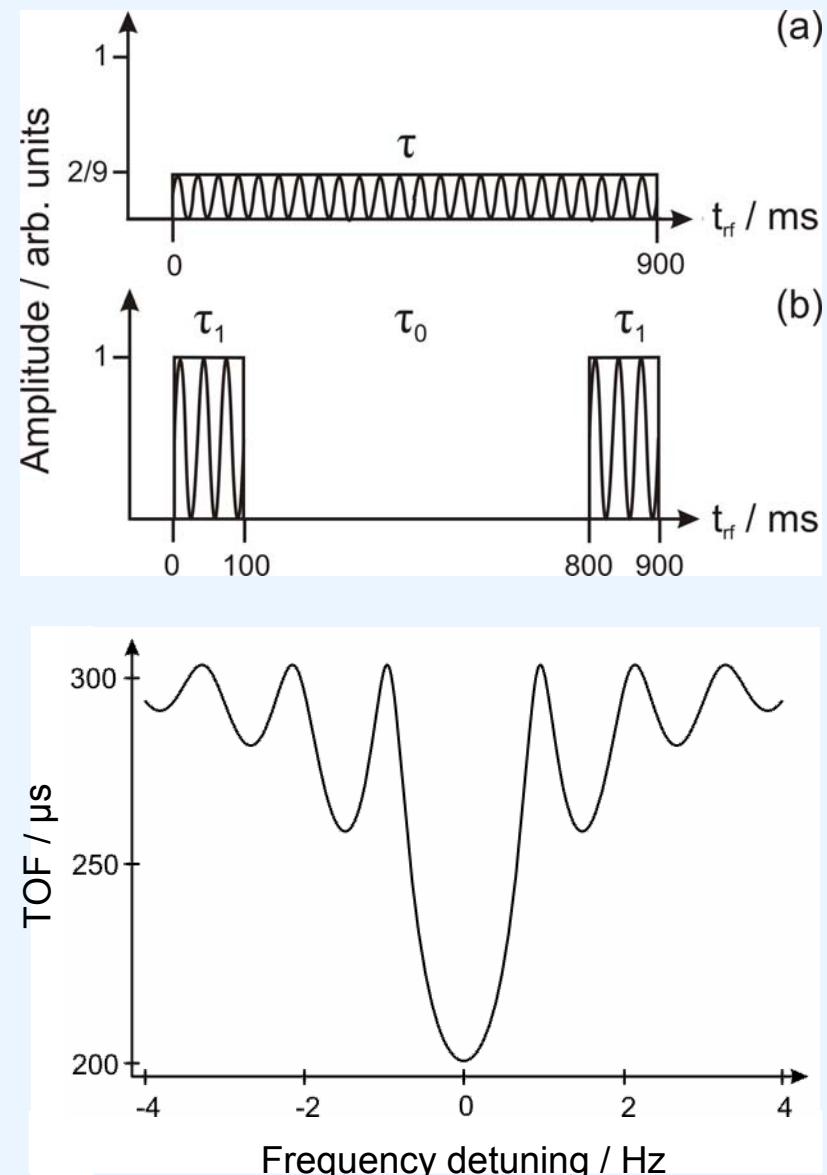
Measurement time: between 15 min and 4 h with ~50-100 ions/s



Determine atomic mass from frequency ratio
with a well-known “reference mass”.

$$\frac{f_{c,\text{ref}}}{f_c} = \frac{m - m_e}{m_{\text{ref}} - m_e}$$

The Ramsey excitation technique

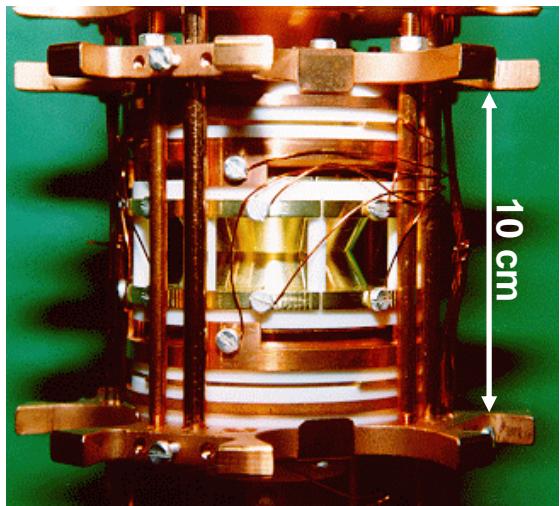


A precision gain of about a factor of 4 is obtained.

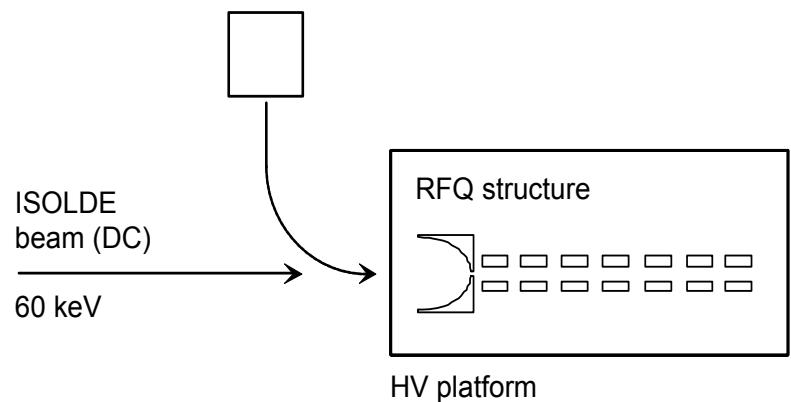
S. George *et al.*, Phys. Rev. Lett. 98, 162501(2007)

Triple-trap mass spectrometer ISOLTRAP

M
A
T
S

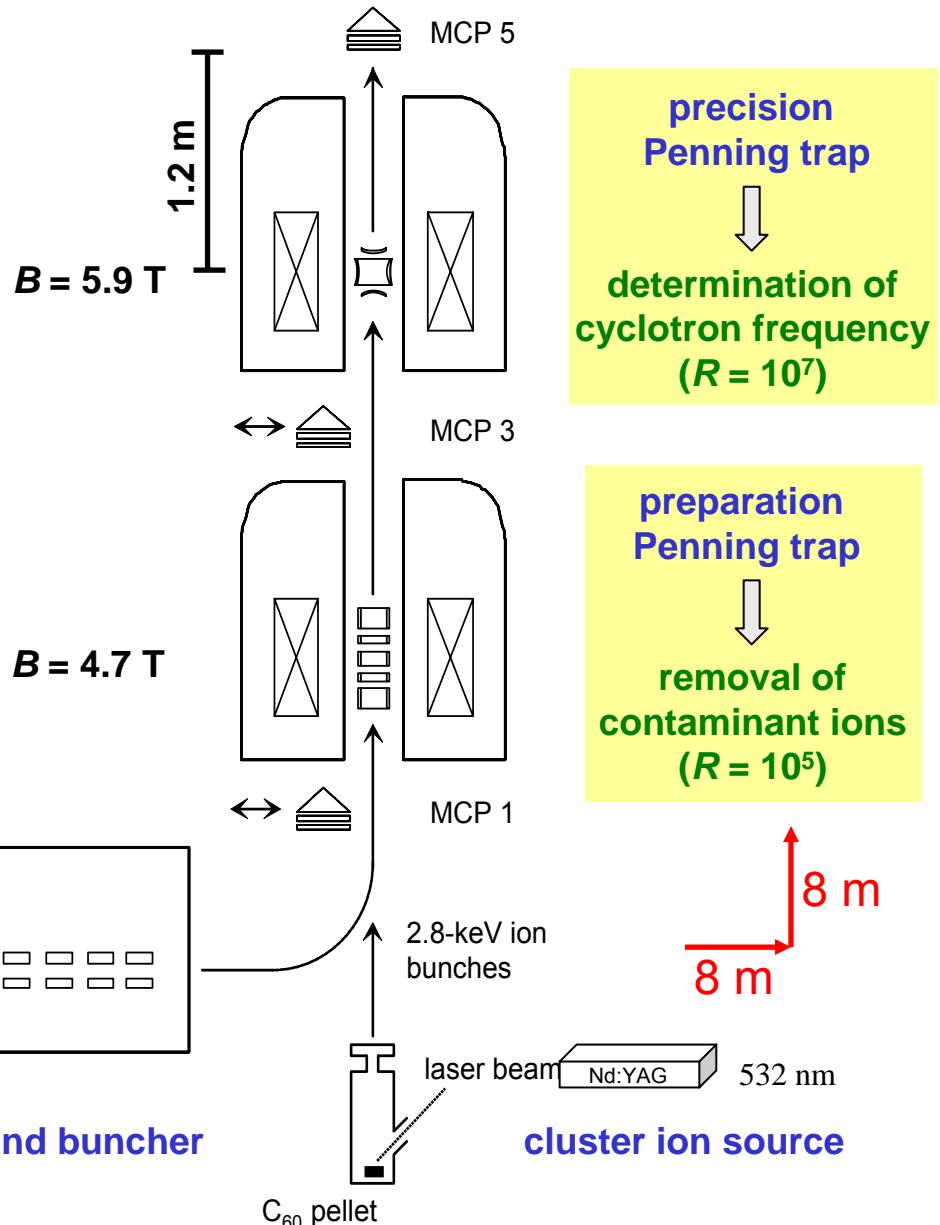


stable alkali ion reference source



ion beam cooler and buncher

F. Herfurth, et al., NIM A 469, 264 (2001)
K. Blaum et al., NIM B 204, 478 (2003)

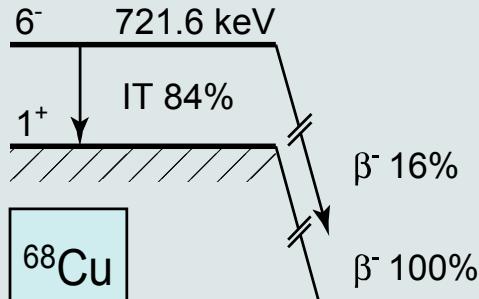


cluster ion source

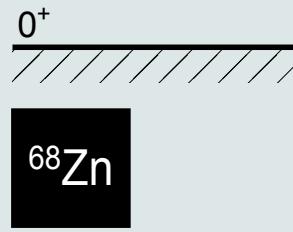
Resolution and isolation of nuclear isomers



Isomerism in ^{68}Cu :



g: $T_{1/2} = 31.1$ s
m: $T_{1/2} = 3.75$ min



K. Blaum et al., Europhys. Lett. 67, 586 (2004)

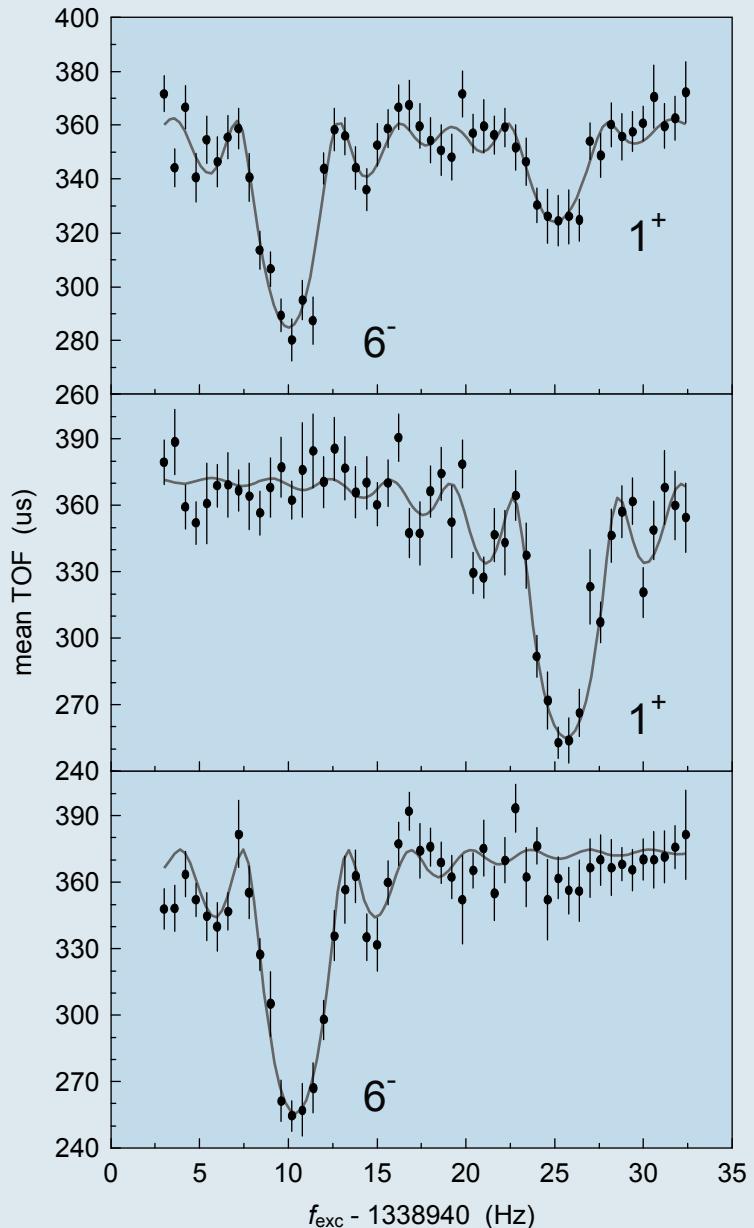
as produced
by ISOLDE

isolation of the
 1^+ ground state

isolation of the
 6^- isomeric state

Applications

- Preparation of an isomerically pure beam
- Clear state-to-mass assignments
- Trap-assisted decay and laser spectroscopy



Isobaric Multiplet Mass Equation

Mass formula for multiplets of nuclear states with same mass and isospin

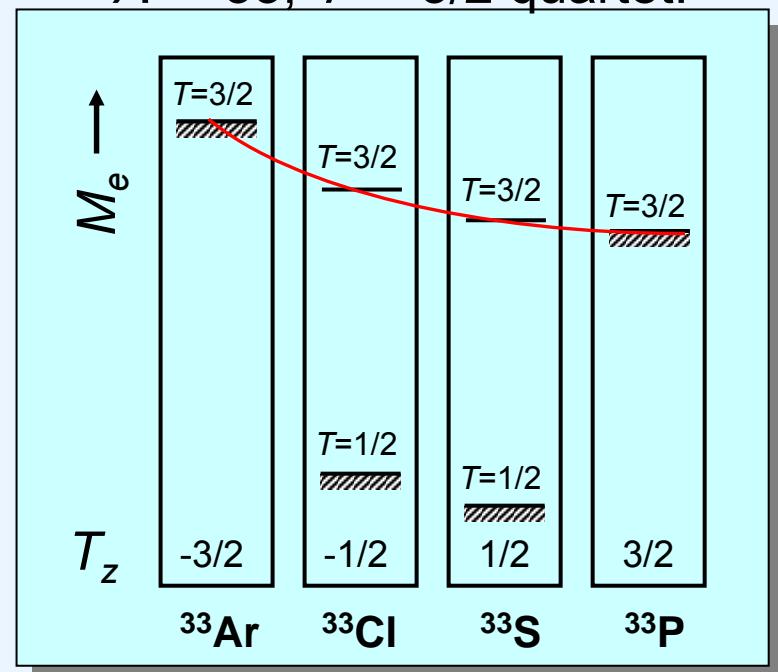
$$M = a + bT_z + cT_z^2$$

$$+ dT_z^3$$

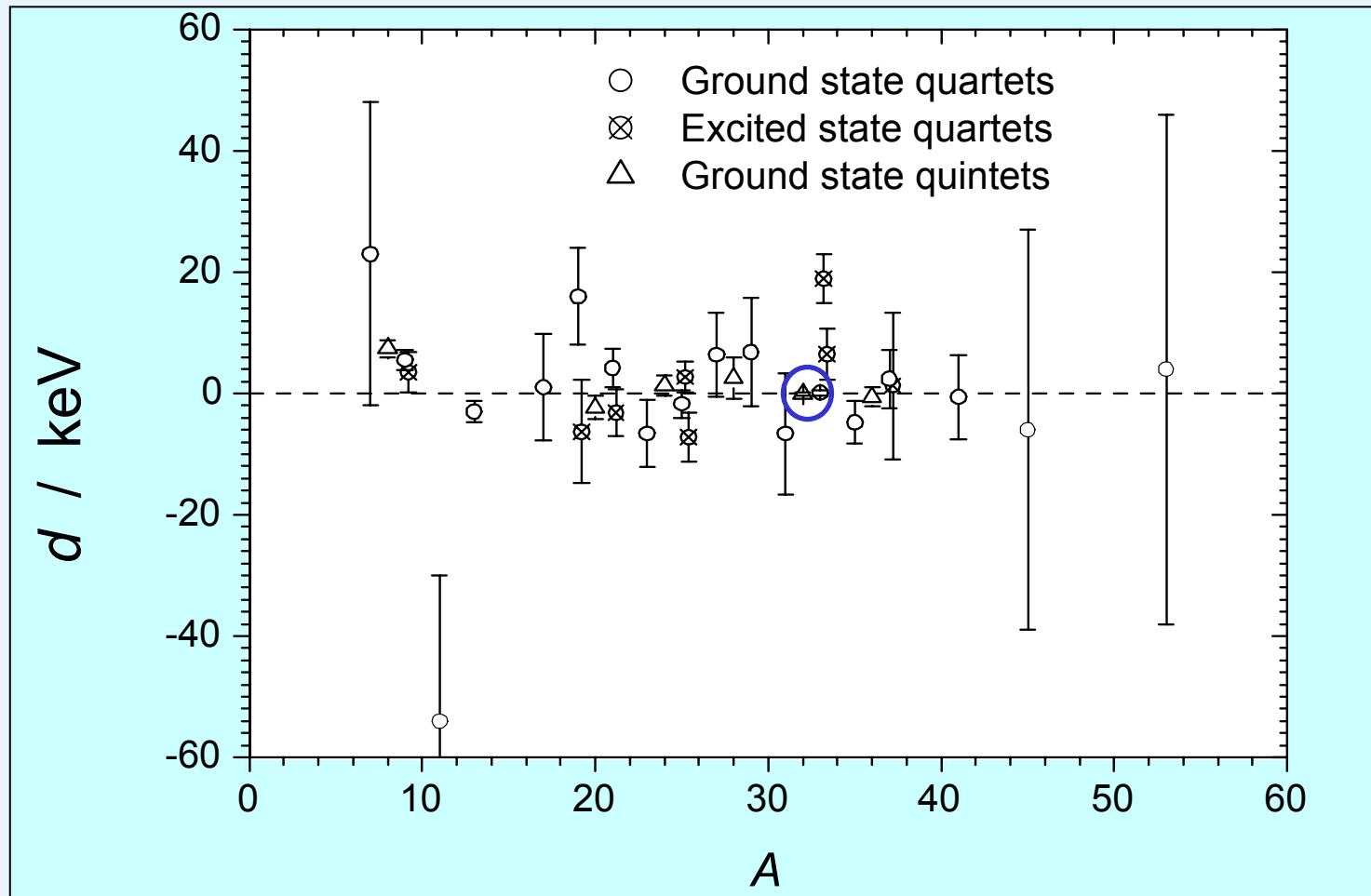
Commonly used quadratic form

?

$A = 33, T = 3/2$ quartet:



Most stringent test of IMME (with $^{32,33}\text{Ar}$)



ISOLTRAP measurements 2002:

- ^{33}Ar with $u(m) = 0.44$ keV
- ^{32}Ar with $u(m) = 1.8$ keV

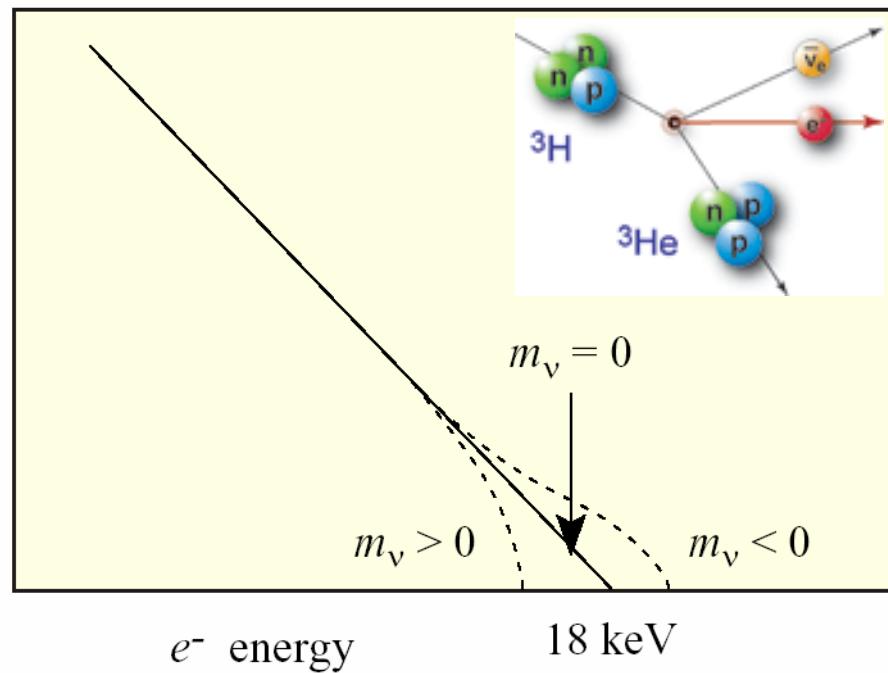
New status:

- | | |
|----------------------------|---------------------|
| $A = 33, T = 3/2$ quartet: | $d = -0.13(45)$ keV |
| $A = 32, T = 2$ quintet: | $d = -0.11(30)$ keV |

K. B. et al., Phys. Rev. Lett. 91, 260801 (2003).

Determination of the ${}^3T \rightarrow {}^3He$ Q-Value

Important parameter for the determination of the electron neutrino rest mass.

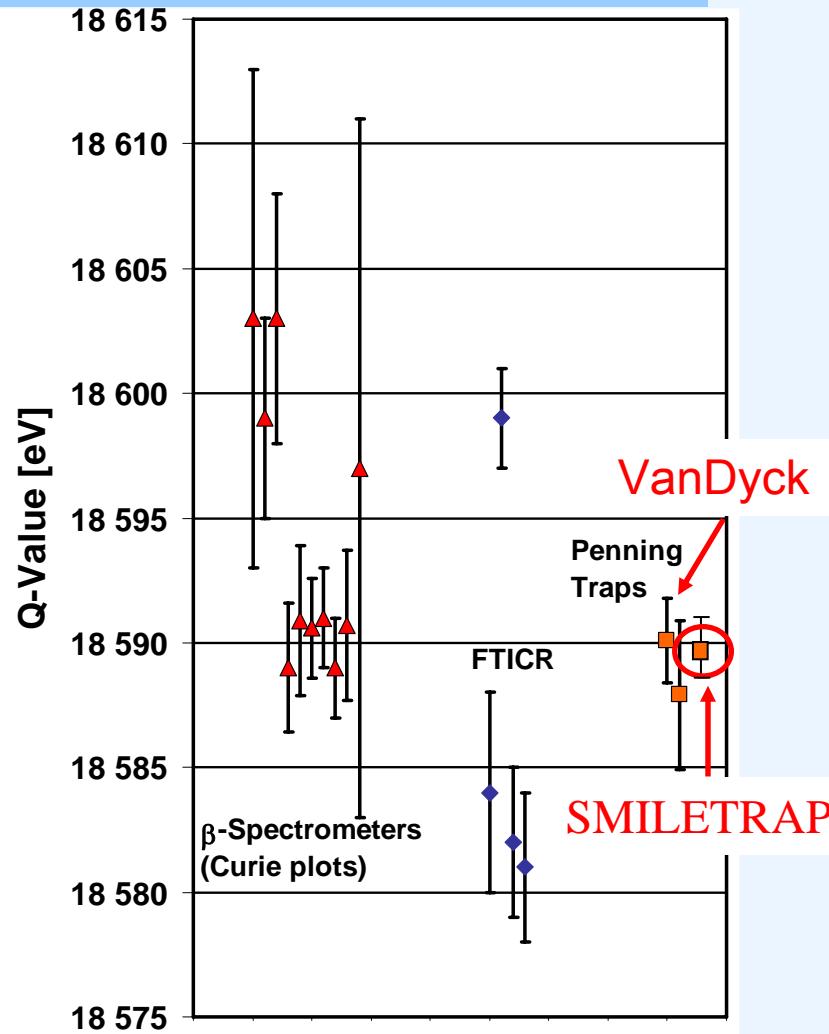


- Q-value of Tritium beta decay



$$Q=18\ 589.8\ (1.2)\ \text{eV}$$

Sz. Nagy *et al.*, Europhys.Lett. 74, 404 (2006)



$$m({}^4\text{He}) = 4.002\ 603\ 254\ 153\ (64) \text{ u} \quad \text{R.S. Van Dyck } et al., \text{ Phys. Rev. Lett. 92 (2004) 220802}$$

Recent results of fundamental studies

M
A
T
S

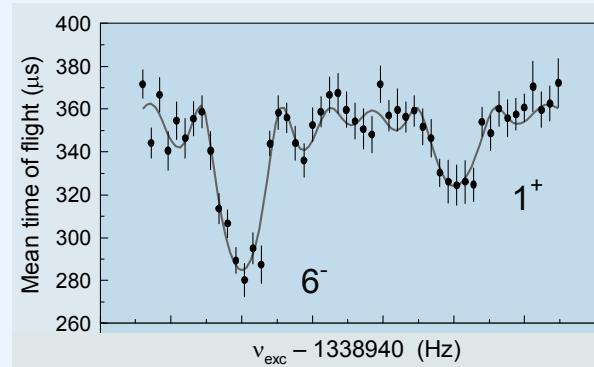
Population inversion of nuclear states and nuclear structure studies:

J. Van Roosbroeck *et al.*, Phys. Rev. Lett. 92, 1112501 (2004)

K. Blaum *et al.*, Europhys. Lett. 67, 586 (2004)

Sz. Nagy *et al.*, Phys. Rev. Lett. 96, 163004 (2006)

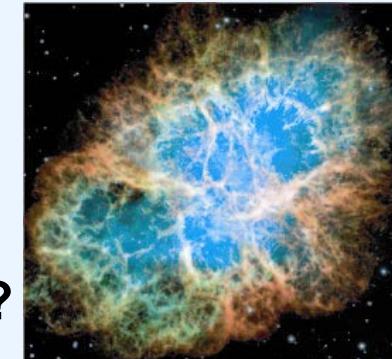
C. Rauth *et al.*, Phys. Rev. Lett., submitted (2007)



Why are there elements heavier than iron?

D. Rodríguez *et al.*, Phys. Rev. Lett. 93, 161104 (2004)

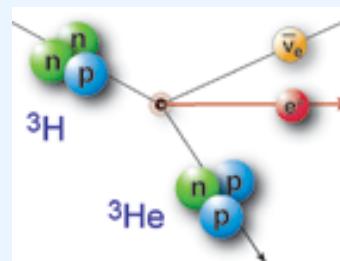
M. Mukherjee *et al.*, Phys. Rev. Lett. 93, 150801 (2004)



Are there scalar currents present in the Weak Interaction?

F. Herfurth *et al.*, Phys. Rev. Lett. 87, 142501 (2001)

K. Blaum *et al.*, Phys. Rev. Lett. 91, 260801 (2003)



V_{ud} – is unitarity violated in quark mixing?

F. Herfurth *et al.*, Eur. Phys. J. A 15, 17 (2002)

A. Kellerbauer *et al.*, Phys. Rev. Lett. 93, 072502 (2004)

M. Mukherjee *et al.*, Phys. Rev. Lett. 93, 150801 (2004)

S. George *et al.*, Phys. Rev. Lett. 98, 162501 (2007)

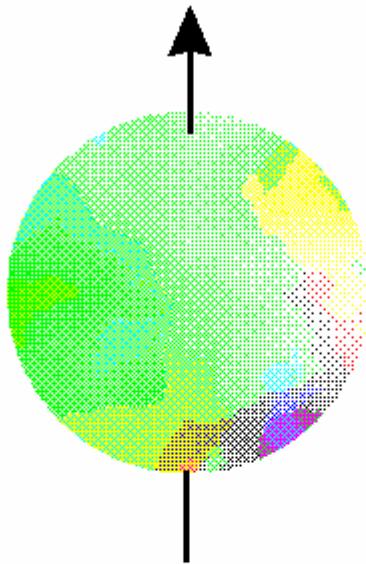
$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \cdot \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

Part II



High-precision *g*-factor measurements

The g – factor



relation between magnetic
dipole moment and angular
momentum

$$\vec{\mu} = g_J \frac{|q|}{2m} \hbar \vec{J}$$

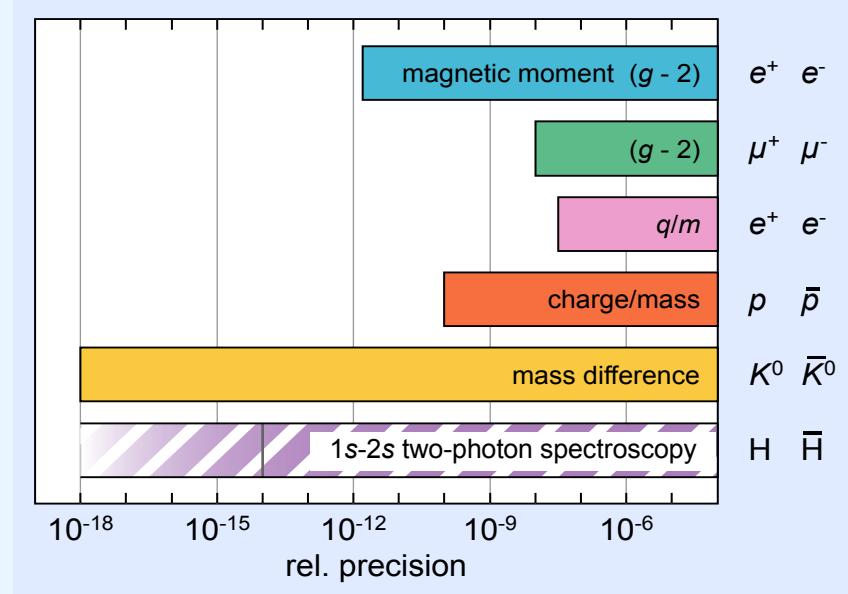
free lepton: g_s = g-factor of the spin

g-factor of the proton and the antiproton

Test of CPT invariance

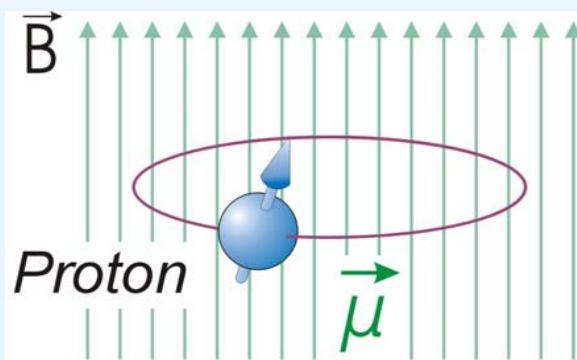
CPT $|\psi\rangle$: Reversal of space,
charge, and time

- Currently believed to hold
- CPT transforms particle into its antiparticle (P. Dirac 1928)

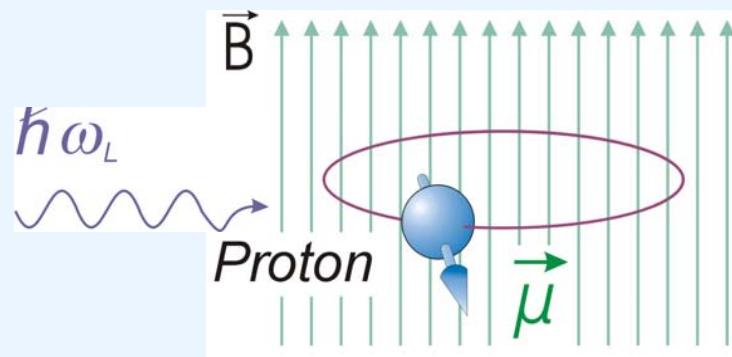


PDG: $g_p = 2 \times 2.792847337(29)$

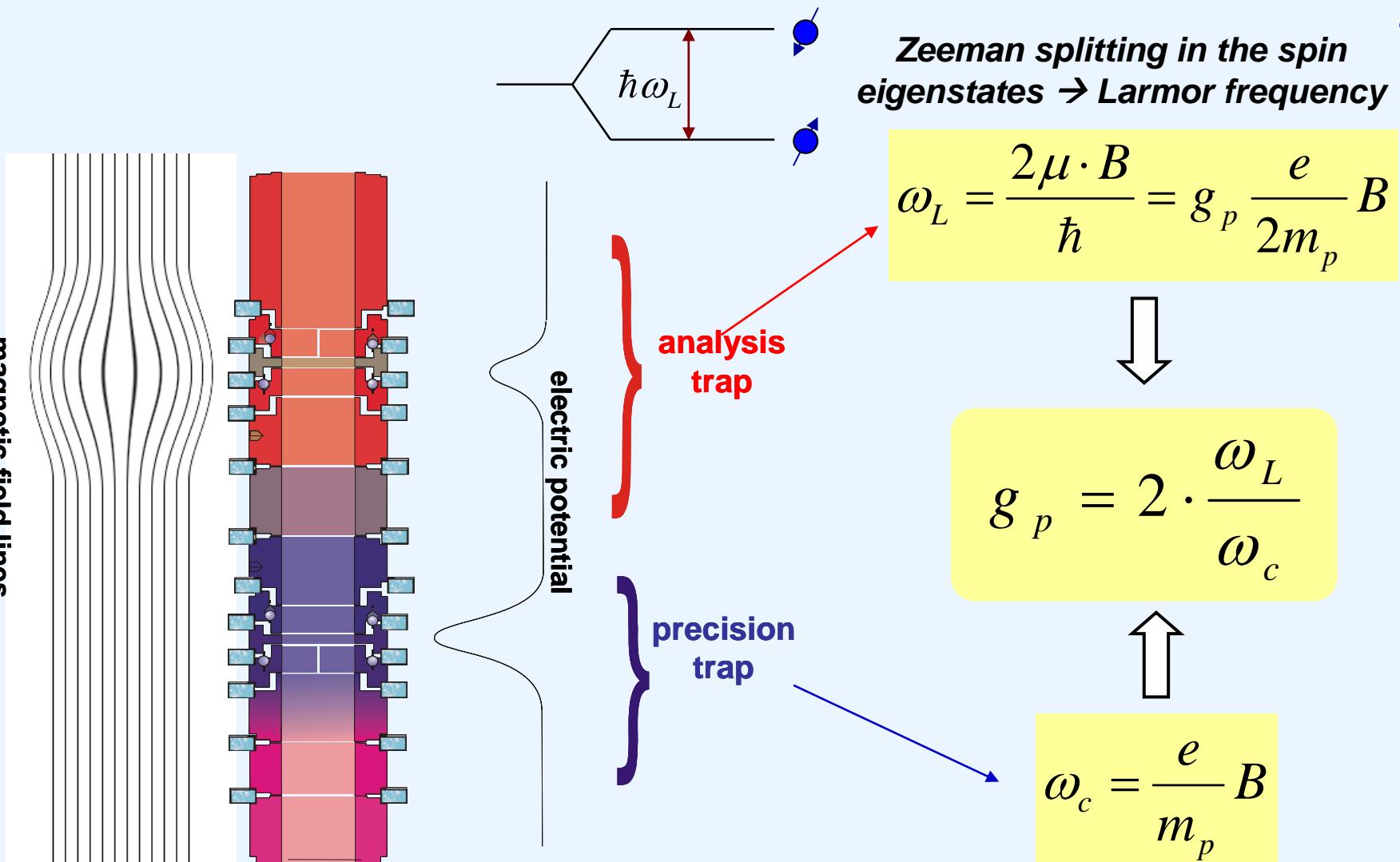
$g_p = 2 \times 2.800(8)$



$$\frac{|\overline{\mu}_p|}{\mu_N} = g_p \cdot \frac{|\overline{s}|}{\hbar}$$



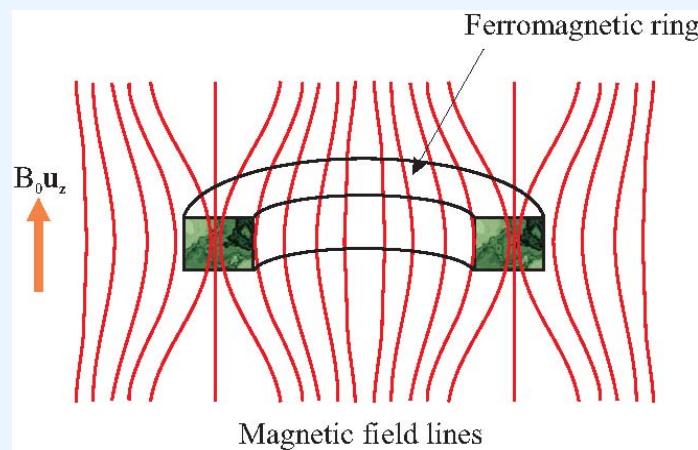
Measurement principle for a proton



We aim for $\delta g/g < 10^{-9}$.

Eigenmotions of the particle → cyclotron frequency

Measurement of the Lamor frequency

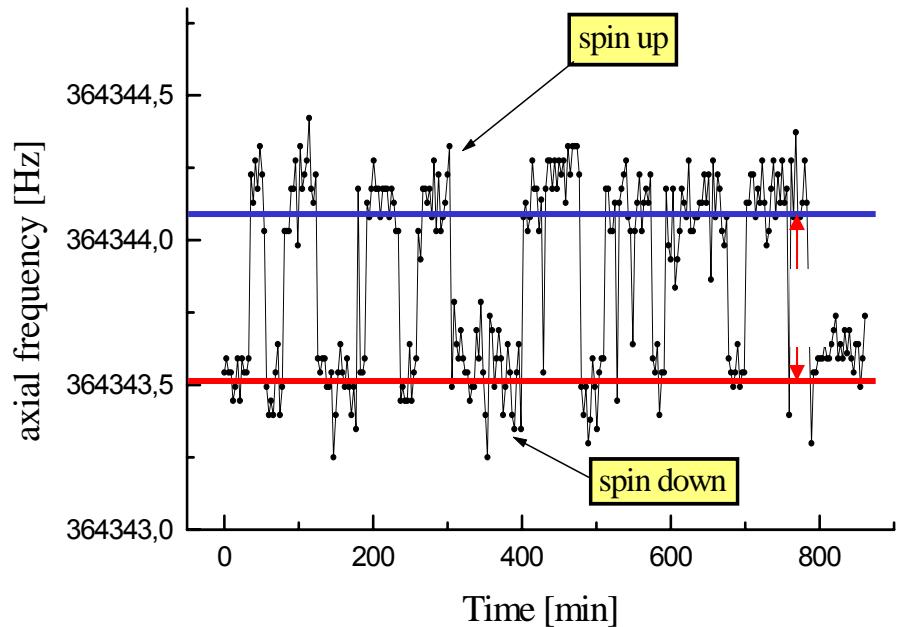
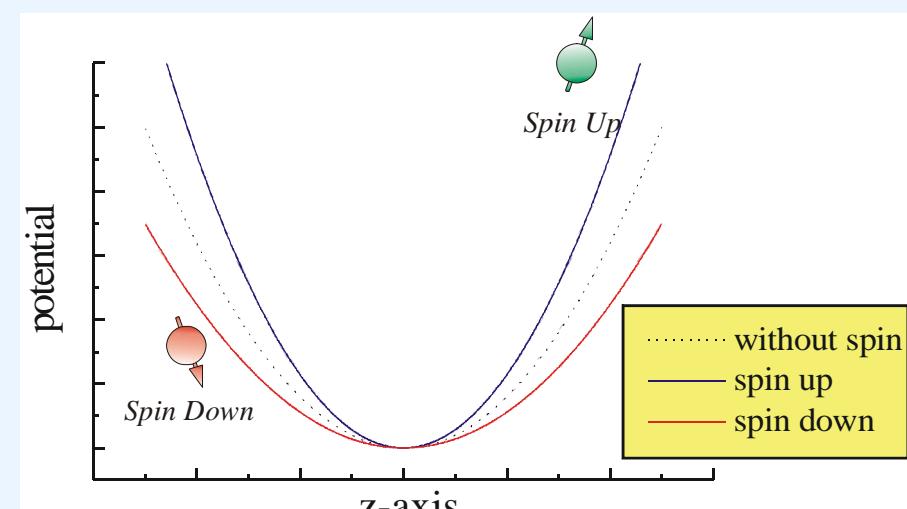


magnetic bottle



$$V_{mag} = -\vec{\mu} \cdot \vec{B} = \mp |\mu| (B_0 + B_2 z^2 + \dots)$$

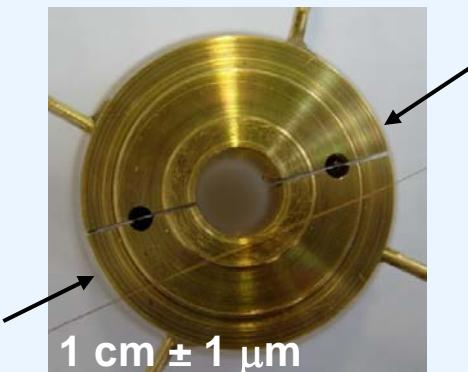
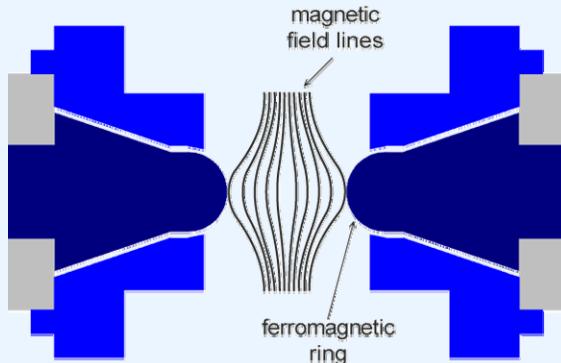
$$\Delta \omega_z = \frac{B_2}{m \cdot \omega_z} \cdot g \cdot \mu_B$$



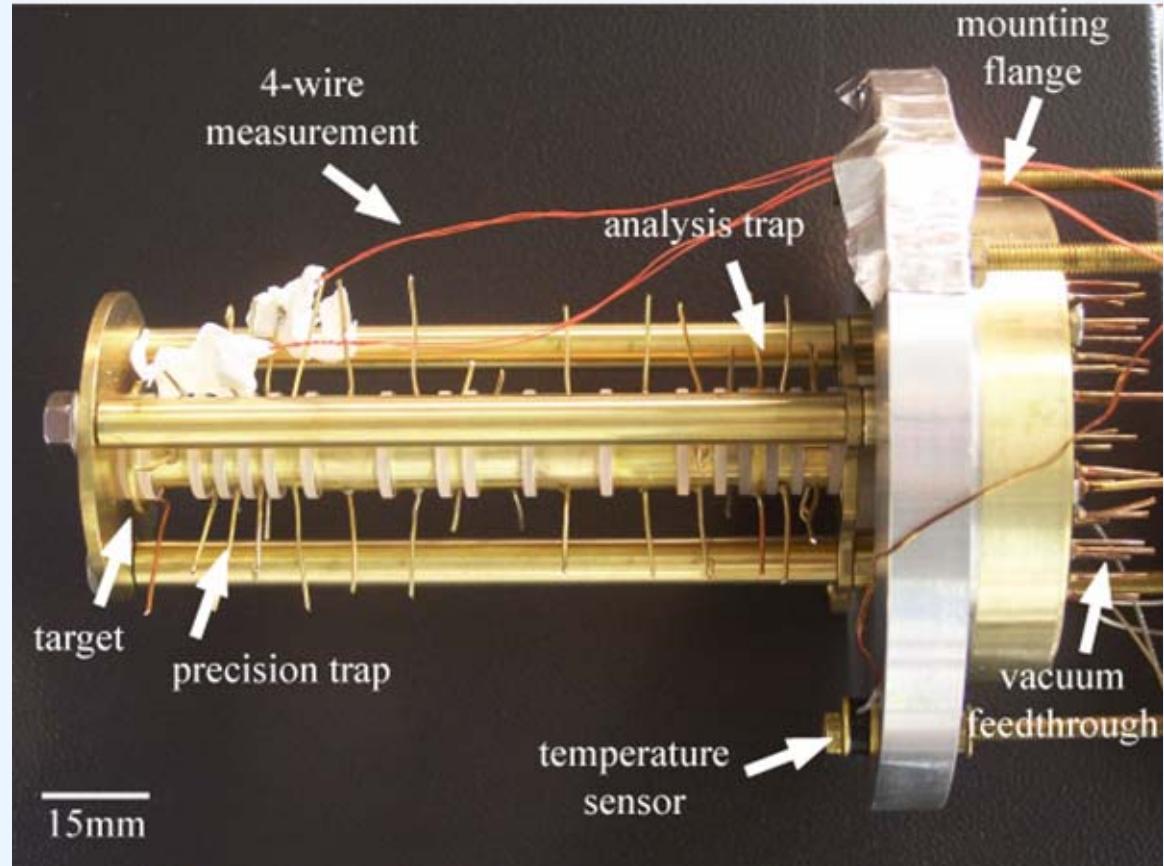
spin-flips result in measurable axial frequency jumps

Status of the (anti)proton g-factor experiment

Hybrid analysis trap



Manufactured at the
Institute for Microtechnique
Mainz (IMM).



Summary

High-accuracy experiments with stored ions in Penning traps have a broad range of applications!

- Fundamental tests:
 - Unitarity test of the CKM matrix: [Hardy & Towner, PRL 94, 092502 (2005)]
 $\delta m/m < 10^{-8}$ for short-lived radionuclides ($T_{1/2} < 100$ ms)
 - Test of $E=mc^2$: [S. Rainville et al., Nature 438, 1096 (2005)]
 $\delta m/m < 10^{-10}$ for ^{32}S , ^{33}S
 - Test of CPT invariance: [G. Gabrielse et al., PRL 82, 3198 (1999)]
 $\delta g/g < 10^{-9}$ for proton and antiproton
 - Test of bound-state QED [J. Verdú et al. PRL 92, 093002 (2004)]
 $\delta g/g < 10^{-9}$ for hydrogen-like highly-charged ions
- Fundamental constants: m_e , m_p , α , $N_a h$, μ , ... [G. Gabrielse et al., PRL 97, 030802 (2006)]

Thanks a lot for your attention.