

# Overview of CP Violation in the Quark Sector

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# Outline

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- Introduction to CP violation
  - Definitions and Background
  - CP Violation in the Flavor sector of Standard Model:  
CKM Matrix, Unitarity Triangle
  - Experimental Physics Goals
- How do we do measurements?
- A few Major Experimental Results
- Conclusion
  - What do we know today?
  - Future

# Definitions and Background

- **Symmetry:** Transformation of a system that does not change the physics laws formulation for this system

**CP:**  
the two  
applied  
consec-  
utively

- **The Parity P:** Inversion of the spatial coordinates, image in a mirror
- **The Charge conjugation C:** Change of all the charge quantum numbers into their opposite, transforms a particle into its anti-particle

$$\vec{x} \rightarrow -\vec{x}$$

$$q_i \rightarrow -q_i$$

**CP Violation**  $\Leftrightarrow$  the world is not symmetric under CP transformation

In the **Standard Model** of Particle Physics (SM):

- **C** and **P** are symmetries of strong and electromagnetic interactions.
- **C** and **P** symmetries are violated by weak interaction
- **CP** symmetry is slightly violated by weak interaction

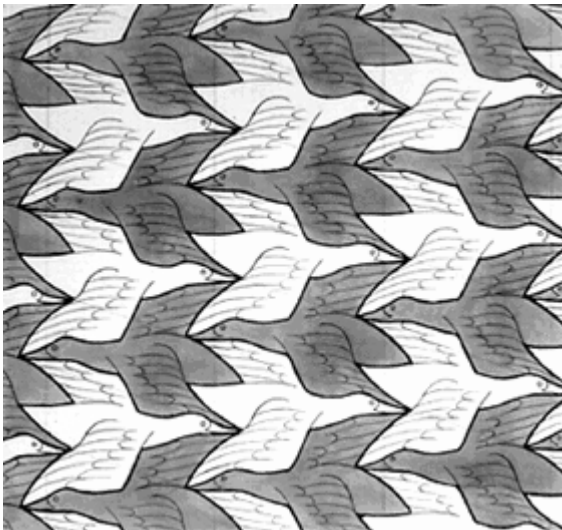
# CP Violation with Escher's Images

**CP** (anti-matter in a mirror)

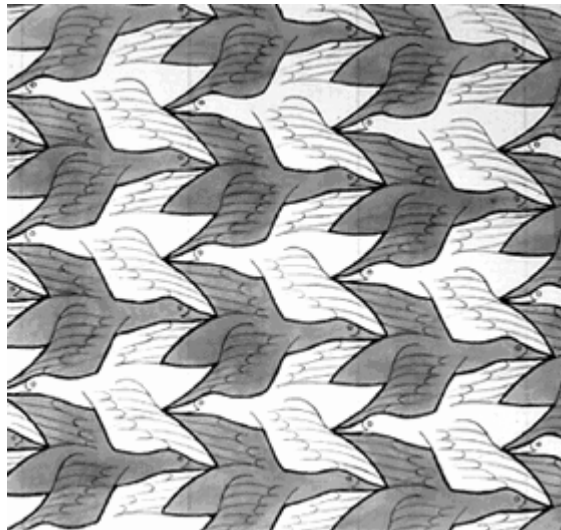
**P** (mirror)

**C** (anti-matter)

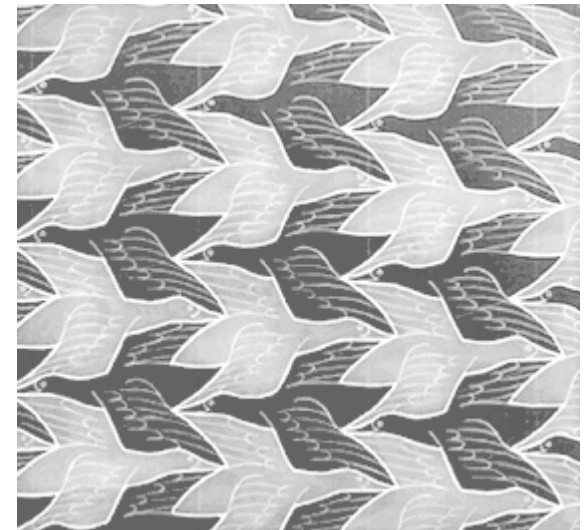
White geese fly right



White geese fly left



White geese fly right



Slight breaking of CP (look at the tails...)

Analogy to weak interaction in the Standard Model.

# The CKM Matrix

In the Quark sector: **Weak Int. eigenstates**  $\neq$  **Mass eigenstates**

$\Leftrightarrow$  **Quarks that participate in weak processes** are linear combinations of **mass eigenstates**

$\Leftrightarrow$  Existence of 3X3 unitary matrix describing the **mixing of quarks**: the **CKM Matrix**

The CKM Matrix:

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix}_J = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}_M$$

CKM matrix

$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

Wolfenstein parameterization:

$$\begin{pmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{\lambda^2}{2} & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

Expansion in powers of  $\lambda$  at the order  $\lambda^3$  with  $\lambda = \sin(\theta_{\text{cabibbo}}) \approx 0.22$

~ half of  
the SM

10 free parameters in the Flavor sector of the SM

6 quark masses

4 CKM parameters (Wolfenstein :  $\lambda, A, \rho, \eta$ )

# From CKM Matrix to Unitarity Triangle

CKM matrix

$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

Wolfenstein parameterization:

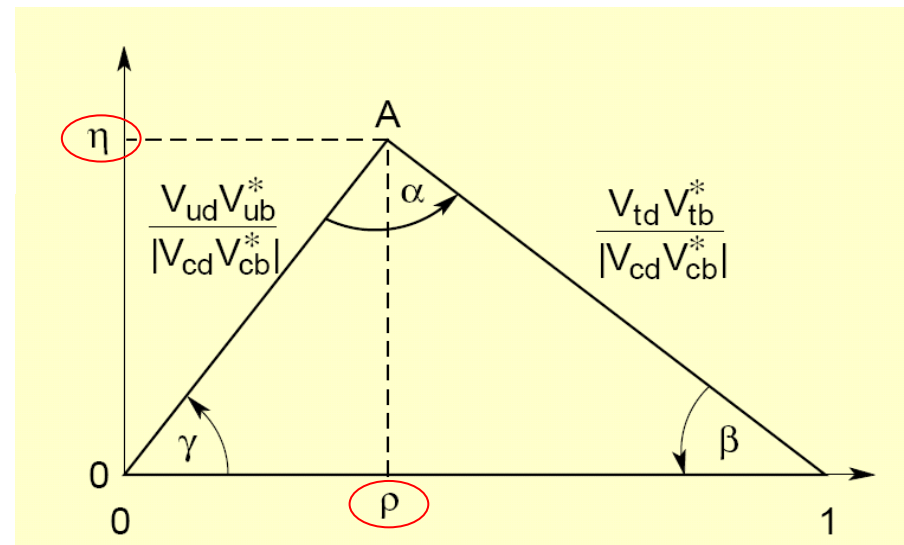
$$\simeq \begin{pmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{\lambda^2}{2} & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

$V_{\text{CKM}}$  Unitarity  $\Rightarrow$

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$

$\propto \lambda^3 \quad \propto \lambda^3 \quad \propto \lambda^3$

Other unitarity conditions (triangles) are difficult to use: Sides are very different. Try it with second and third columns...



CP Violation is possible in the Standard Model only if  $V_{\text{CKM}}$  is complex  $\Leftrightarrow \eta \neq 0 \Leftrightarrow$  Unitarity Triangle is not flat

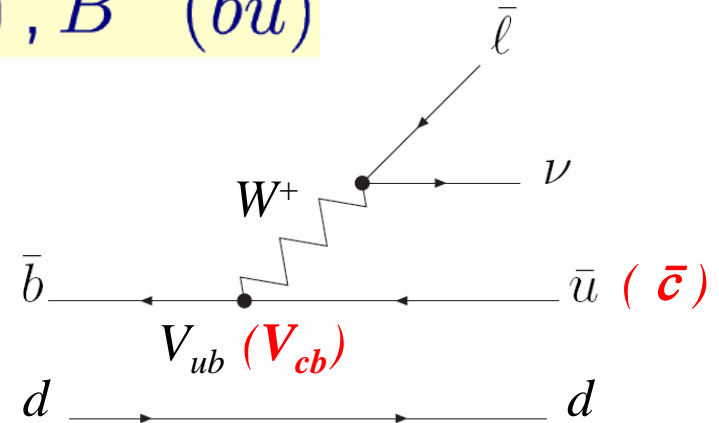
**We want to determine  $\rho$  and  $\eta$  experimentally**

# Examples of Weak Processes

$$B^0 (\bar{b}d) , \bar{B}^0 (b\bar{d}) , B^+ (\bar{b}u) , B^- (b\bar{u})$$

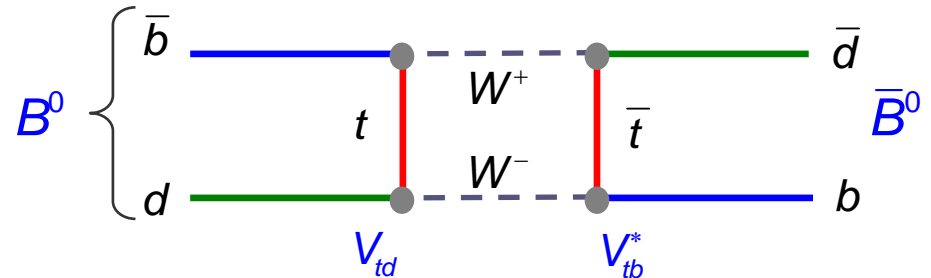
## ■ Semileptonic Decay of $B^0$

Provide information  
on  $V_{ub}$  ( $V_{cb}$ )



## ■ $B^0 \leftrightarrow \bar{B}^0$ Oscillations

$$\propto (V_{td} V_{tb}^*)^2$$



# More on B Oscillations

With the weak int. eigenstates:

$$|B_L\rangle = p|B^0\rangle + q|\bar{B}^0\rangle$$

$$|B_H\rangle = p|B^0\rangle - q|\bar{B}^0\rangle$$

Oscillation frequency, width difference:

$$\Delta M_d = m_{B_H} - m_{B_L}$$

$$\Gamma_d = \Gamma_{B_H} - \Gamma_{B_L}$$

Time evolution of a B meson that was a  $B^0$  at  $t=0$ :

$$|B^0(t)\rangle = e^{-im_B t} e^{-\Gamma_d t/2} \left[ \cos\left(\frac{\Delta m_d t}{2}\right) |B^0\rangle + i \frac{q}{p} \sin\left(\frac{\Delta m_d t}{2}\right) |\bar{B}^0\rangle \right]$$

**Oscillation term**  $\Rightarrow$   $\left[ \cos\left(\frac{\Delta m_d t}{2}\right) |B^0\rangle + i \frac{q}{p} \sin\left(\frac{\Delta m_d t}{2}\right) |\bar{B}^0\rangle \right]$   $\leftarrow$  **Decay term**

## Competition between oscillation and decay

To study oscillations, need to identify the species of the  $B$  meson at time  $t=0$ .  
To follow its time evolution, need to measure time.

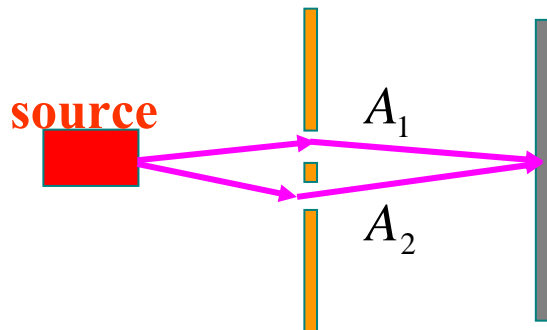


# Two Types of CP Violation

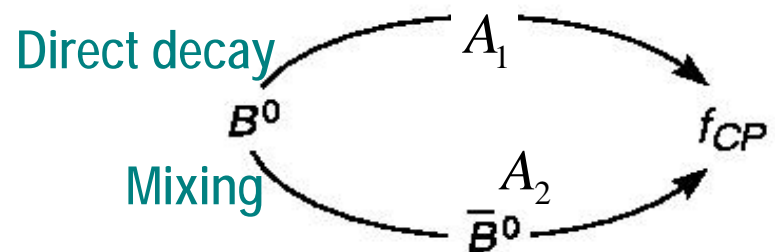
- **Direct CP Violation:**  $B \rightarrow f \neq \bar{B} \rightarrow \bar{f}$ , with  $f \neq \bar{f}$ 
  - To measure it, only need to count events.
  - Rates are different  $\Leftrightarrow$  CP is violated
  - Only type of CP violation for charged B mesons
- **CP violation in the interference between decay and mixing:**

$$B^0 \rightarrow f \neq \bar{B}^0 \rightarrow f$$

Analogy to “Double-Slit” experiment

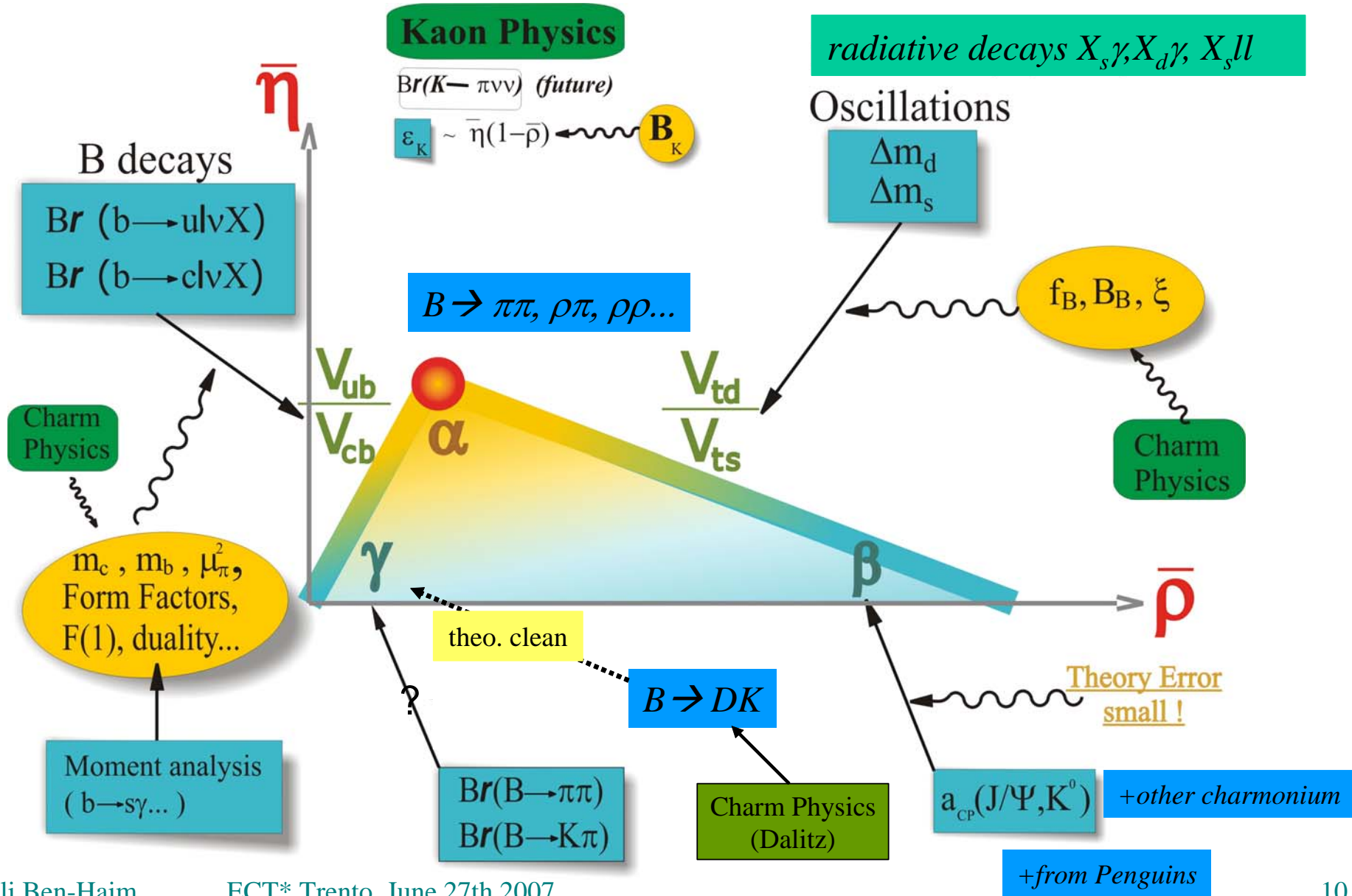


*In the double-slit experiment, there are two paths to the same point on the screen.*

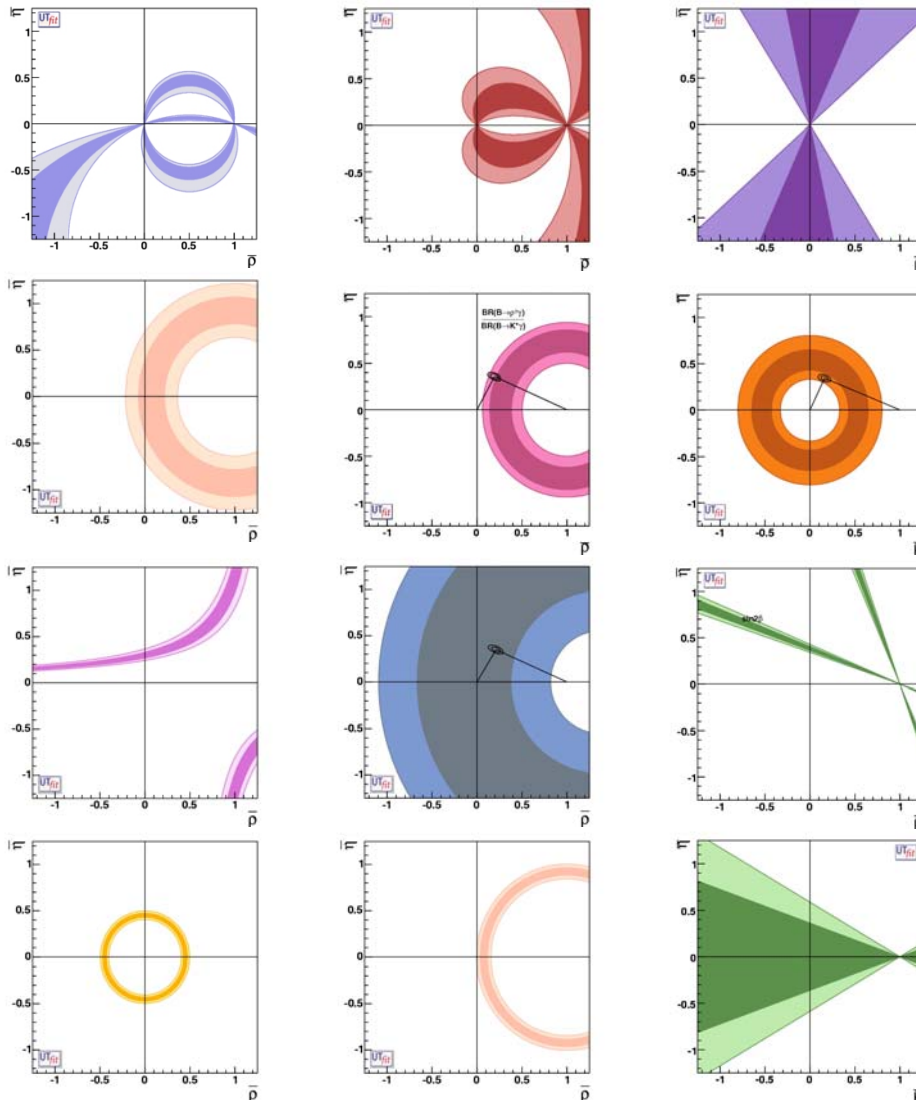


*In the B experiment, we must choose final states into which both a  $\bar{B}^0$  and a  $B^0$  can decay. We perform the B experiment twice (starting from  $B^0$  and from  $\bar{B}^0$ ). We then compare the results.*

# How to Get $\rho$ and $\eta$ from Experiments?



# The Unitarity Triangle Fit



- **Quantify CP Violation within the Standard Model with precision measurements of its angles and sides**
- **Test the Standard Model, by over- constraining the Unitarity Triangle with redundant measurements. If there is New Physics (not described by the Standard Model), we might see some incompatibilities between several independent measurements of the same parameter of the UT.**

# Intermediate Summary, What do We know by Now?

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- CP and CP violation
- CKM Matrix and the Unitarity Triangle
- B mixing
  
- Goals and motivations for studying CP violation:
  - **Constrain the Standard Model by measuring its free parameters. Flavor sector in one of its less known parts before B-Factories**
  - **Test the Standard Model and eventually challenge it by showing discrepancies between several measurements of the same parameters → a window for discovery of New Physics**
  
  - **It is also one of the necessary conditions to explain matter-antimatter asymmetry in the universe**

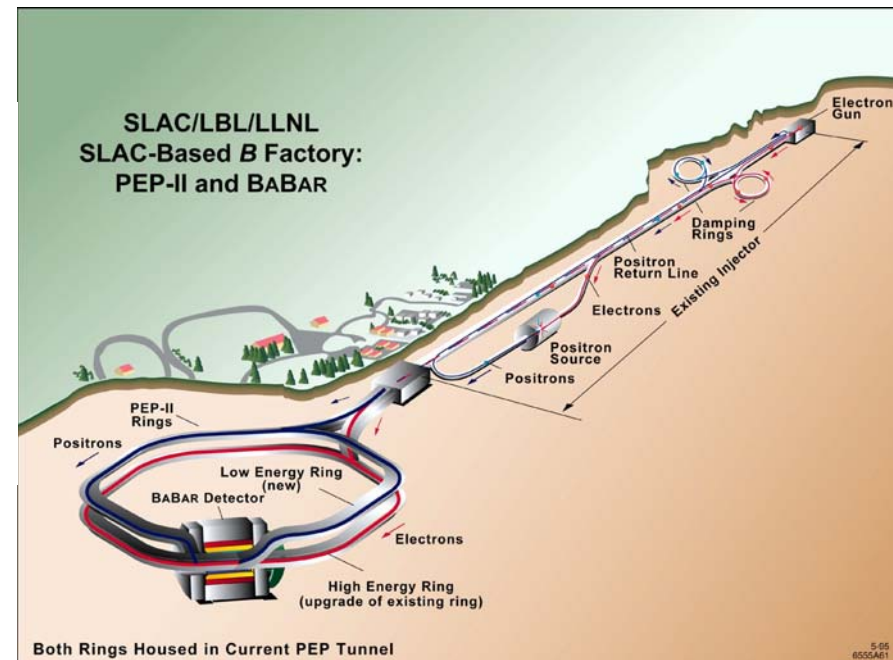
Sakharov, JETP Lett. 5, 24 (1967).

# B-Factories

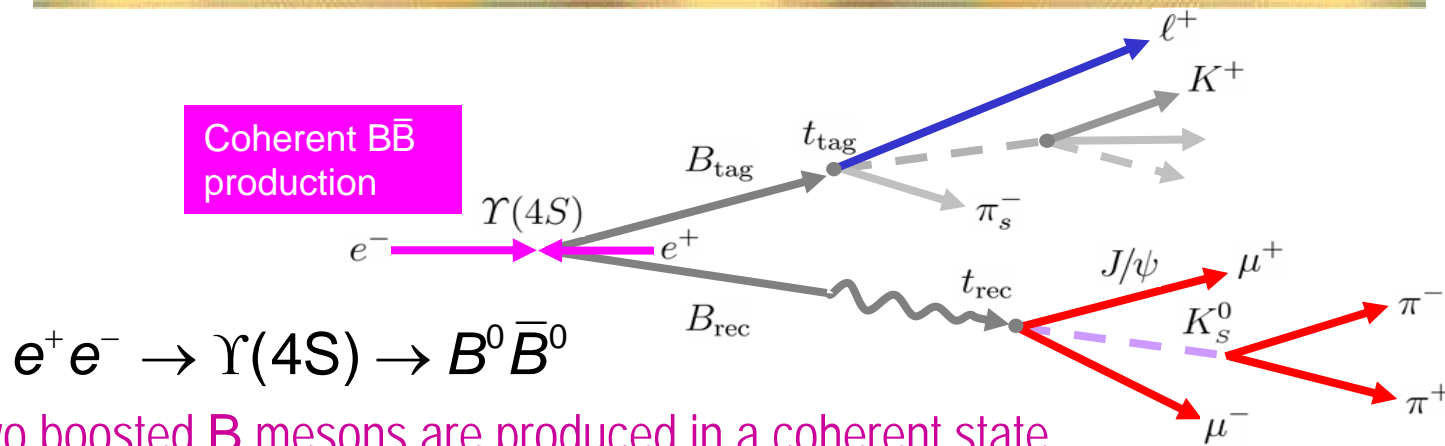
- Experiments designed for precision measurements of CP violation in the B meson (and Charm) sector
- Two active B-Factories experiments:
  - BaBar, in Stanford Linear Accelerator Center (California)
  - Belle, in KEKB (Japan)

- The BaBar experiment:

$e^-(9\text{ GeV})/e^+(3.1\text{ GeV})$  collision  
 $E_{CM} = m(\Upsilon(4S)) = 10.58\text{ GeV}$   
 $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B/\bar{B}$   
almost at rest in the CM frame  
boost of  $\Upsilon(4S)$  with  $\beta\gamma = 0.56$



# Time Dependent Measurements, Flavor Tagging



$$e^+e^- \rightarrow \Upsilon(4S) \rightarrow B^0\bar{B}^0$$

Two boosted **B** mesons are produced in a coherent state  
 $\Rightarrow$  until the first B decay, there is exactly one  $B^0$  and one  $\bar{B}^0$

$$\beta\gamma \sim 0.56$$

$$\Delta t = 1.6 \text{ ps} \Leftrightarrow \Delta z \approx 200, 250 \text{ } \mu\text{m}$$

## Problem:

If we want to study a decay

$$B^0 \rightarrow f$$

Where  $f$  is also accessible by an anti- $B^0$

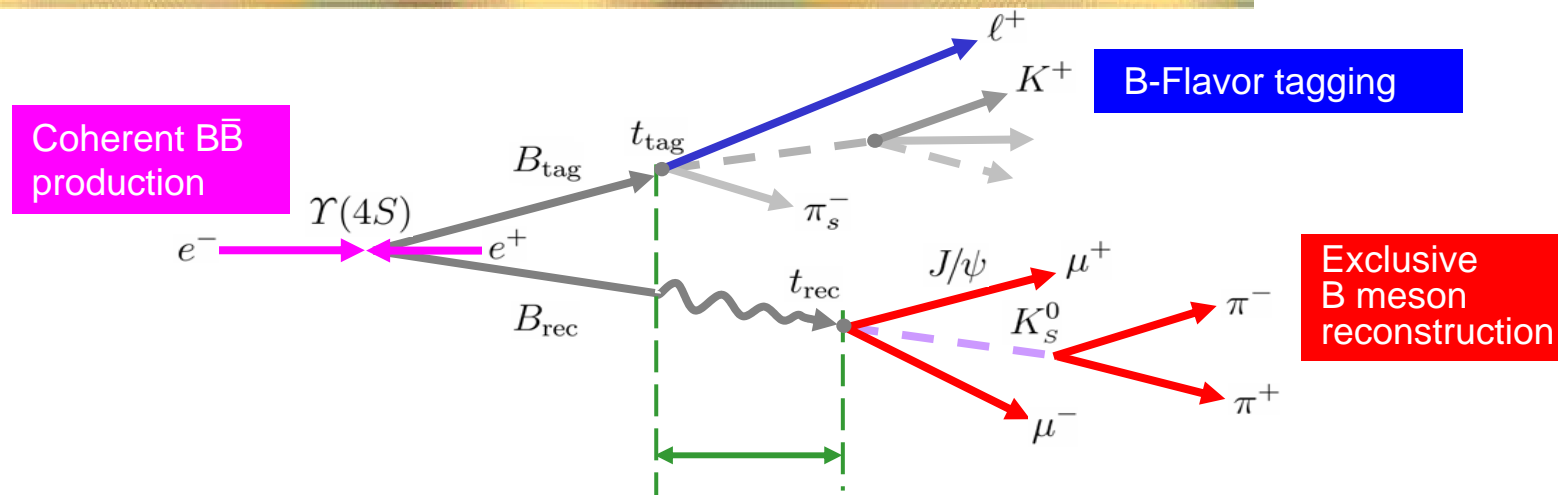
$$\bar{B}^0 \rightarrow f$$

And we want to see if

$$B^0 \rightarrow f \neq \bar{B}^0 \rightarrow f$$

**We need to find a clever way to know the B flavor**

# Time Dependent Measurements, Flavor Tagging



$$\Delta t \equiv t_{\text{rec}} - t_{\text{tag}} \approx \Delta z / \beta\gamma c$$

## Solution:

- There is coherent evolution until  $B_{\text{tag}}$  decays
- At  $t_{\text{tag}}$  the flavor of  $B_{\text{reco}}$  is the opposite of the  $B_{\text{tag}}$ 's flavor
- $B_{\text{reco}}$ 's flavor determined from  $B_{\text{tag}}$ 's flavor and  $\Delta t$
- Boost:  $\Delta t$  measured via space length measurement between  $B_{\text{tag}}$  and  $B_{\text{reco}}$   $\Delta z$
- Flavor of the  $B_{\text{tag}}$  determined by its decay product: charge of leptons, K,  $\pi$

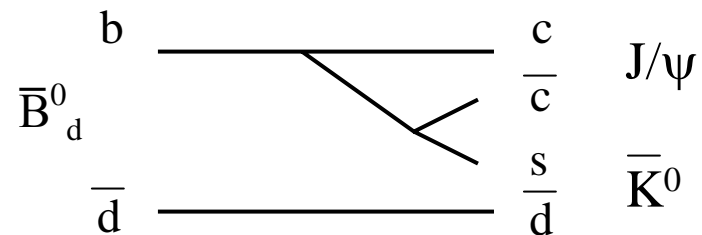
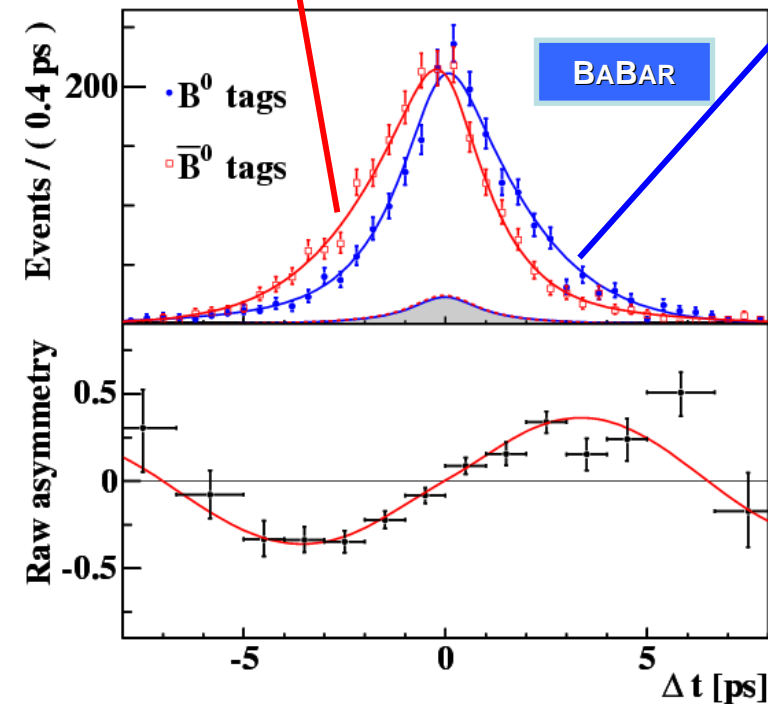


# Measurement of $\sin(2\beta)$ with $B^0 \rightarrow J/\psi K_S^0$

- Final state accessible to  $B^0$  and  $\bar{B}^0 \rightarrow$  Time dependent asymmetry:

$$A_{CP}(t) = \frac{\Gamma(\bar{B}^0(t) \rightarrow J/\psi K_S) - \Gamma(B^0(t) \rightarrow J/\psi K_S)}{\Gamma(\bar{B}^0(t) \rightarrow J/\psi K_S) + \Gamma(B^0(t) \rightarrow J/\psi K_S)} = \boxed{S} \sin(\Delta m_d t) - \boxed{C} \cos(\Delta m_d t)$$

↑ indirect      ↑ direct



~only one amplitude

$$C_f = 0$$

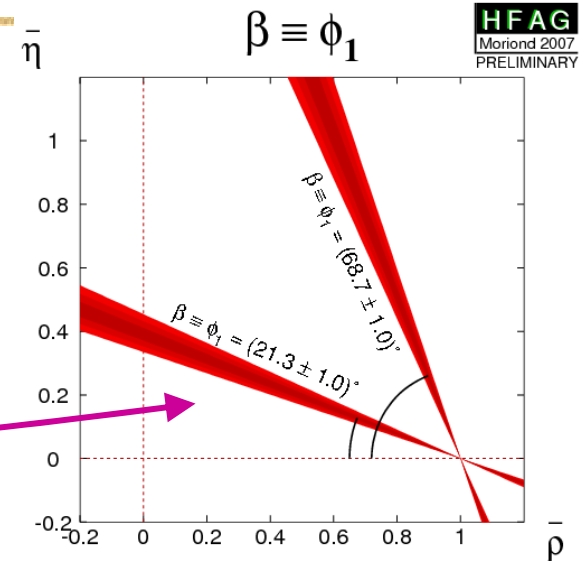
$$S_f = -\eta_{CP} \sin 2\beta$$

$\Rightarrow$  Extraction of  $\sin(2\beta)$  from  $A_{cp}$

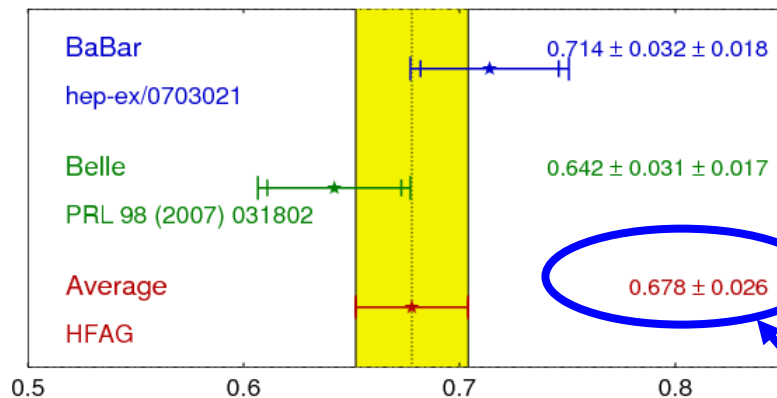


# Measurement of $\sin(2\beta)$ with $B^0 \rightarrow J/\psi K_S^0$

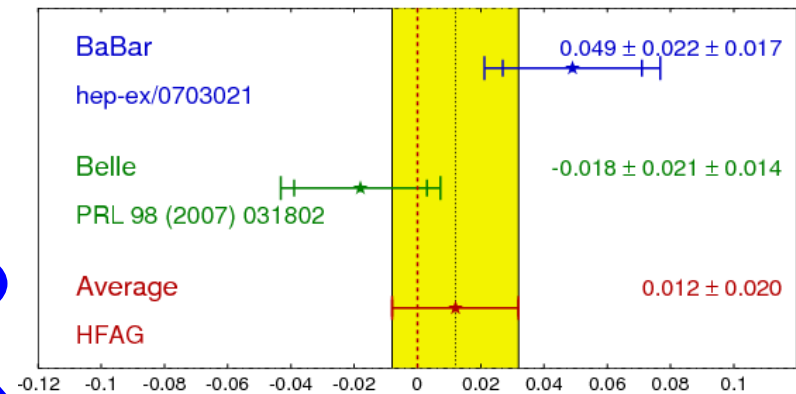
- This measurement is theoretically clean (at 1%)
- Benefits from a large data sample
- $\sin(2\beta)$  gives the best **constraint on  $\rho$ - $\eta$  plane**



$\sin(2\beta) \equiv \sin(2\phi_1)$  HFAG  
Moriend 2007  
PRELIMINARY

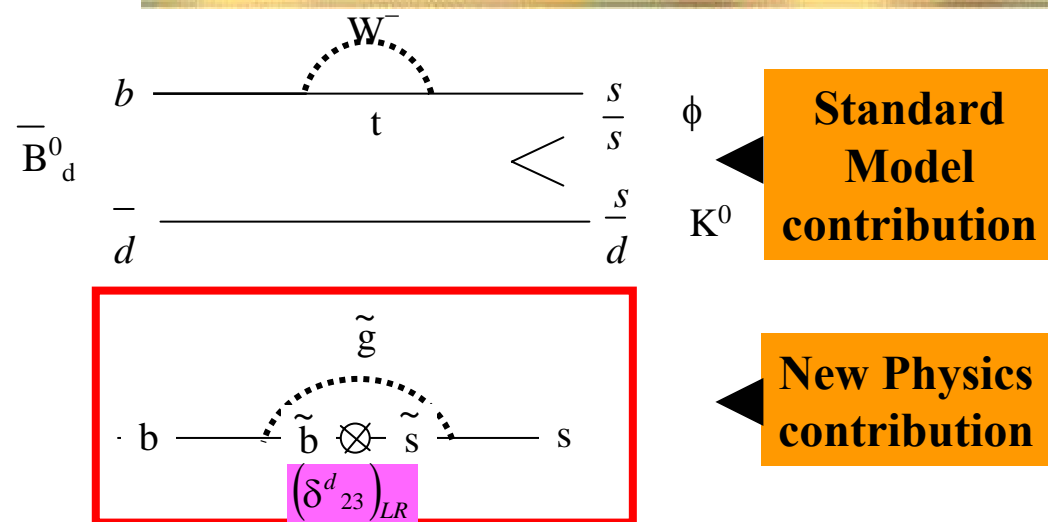


$b \rightarrow ccs$   $C_{CP}$  HFAG  
Moriend 2007  
PRELIMINARY



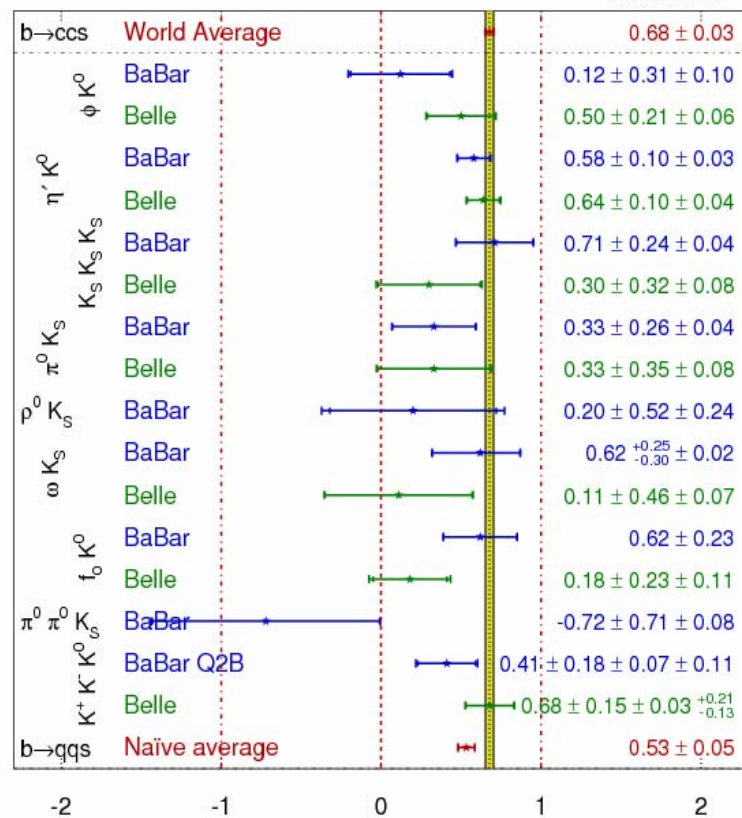
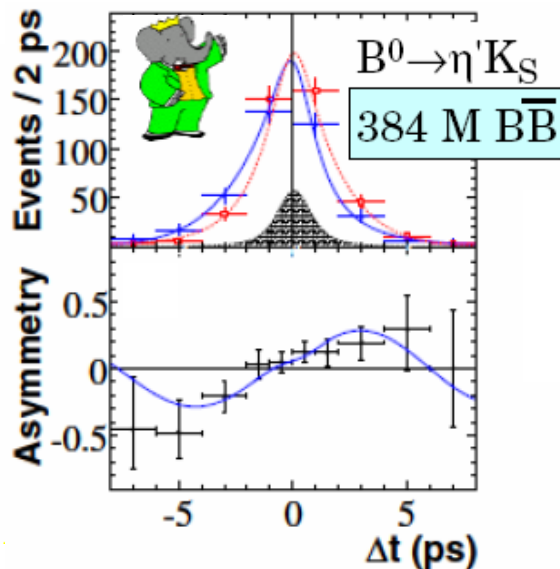
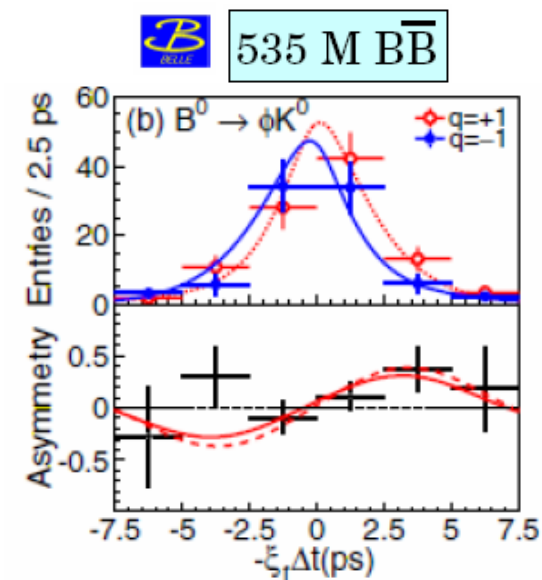
$\sin(2\beta) \neq 0 \Rightarrow$  non flat triangle i.e. CP violation

# Measurement of $\sin(2\beta)$ with “s Penguins”



$$\sin(2\beta^{\text{eff}}) \equiv \sin(2\phi_1^{\text{eff}})$$

**HFAG**  
Moriond 2007  
PRELIMINARY



Tensions between  $\sin 2\beta$  from  $b \rightarrow ccs$  and  $b \rightarrow qqs$

# $B^0_s$ Oscillations: $\Delta m_s$ Measurement at the TeVatron

$$\Delta m_d = 0.509 \pm 0.006 \text{ ps}^{-1}$$

$$\Delta m_s \sim 30 \times \Delta m_d$$

$\Rightarrow$  **Rapid oscillations for  $B^0_s$**

Behavior in proper time

$$P(t)_{B^0 \rightarrow B^0} = \frac{1}{2\tau} e^{-t/\tau} (1 + \cos \Delta m t)$$

$$P(t)_{B^0 \rightarrow \bar{B}^0} = \frac{1}{2\tau} e^{-t/\tau} (1 - \cos \Delta m t)$$

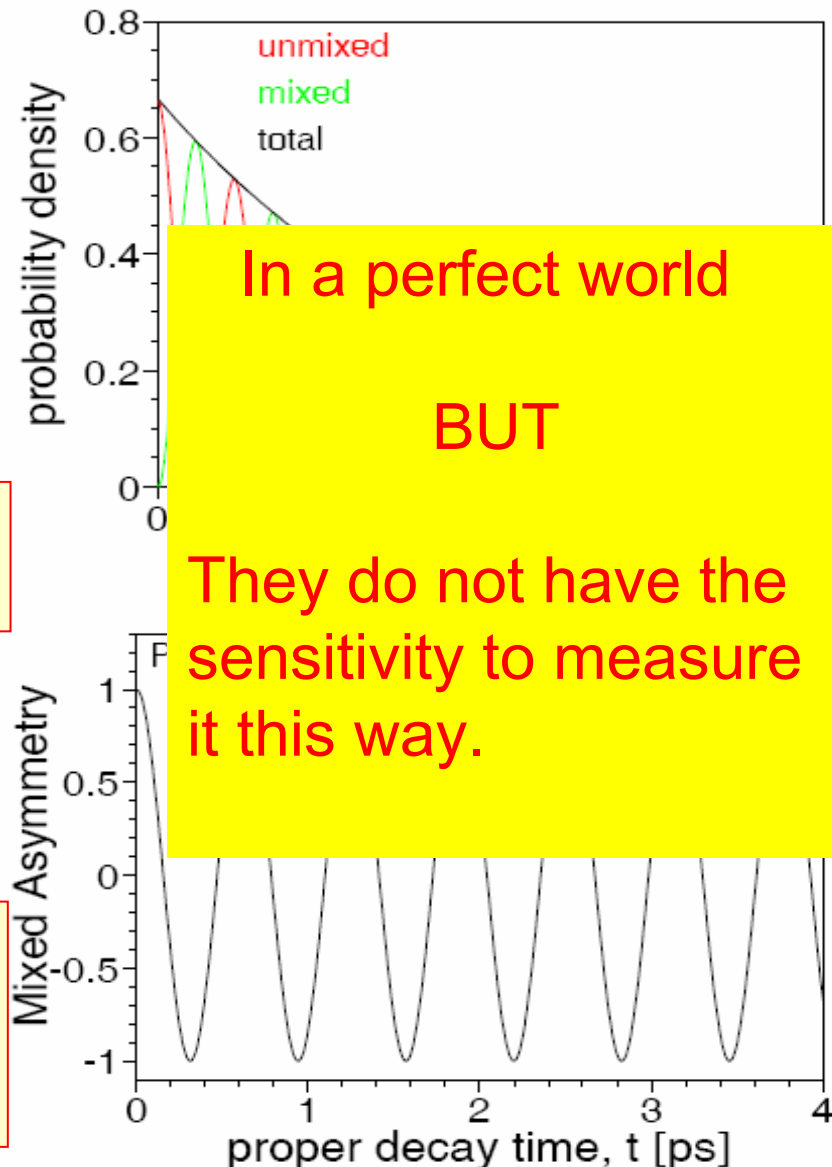
In this case, they are able to determine the flavor at decay and at production

Determine asymmetry

$$A_0(t) = \frac{N(t)_{\text{unmixed}} - N(t)_{\text{mixed}}}{N(t)_{\text{unmixed}} + N(t)_{\text{mixed}}} = \cos \Delta m t$$

• “unmixed”: same flavor at decay and at production

• “mixed”: different flavor



# $\Delta m_s$ Measurement: Fourier Analysis

Two domains to fit for oscillation:

Time domain:

→ fit for  $\Delta m_s$  in  $P(t) \sim (1 \pm D \cos \Delta m_s t)$

Frequency domain: **amplitude scan**

→ introduce amplitude:

$$P(t) \sim (1 \pm \mathcal{A} D \cos \Delta m_s t)$$

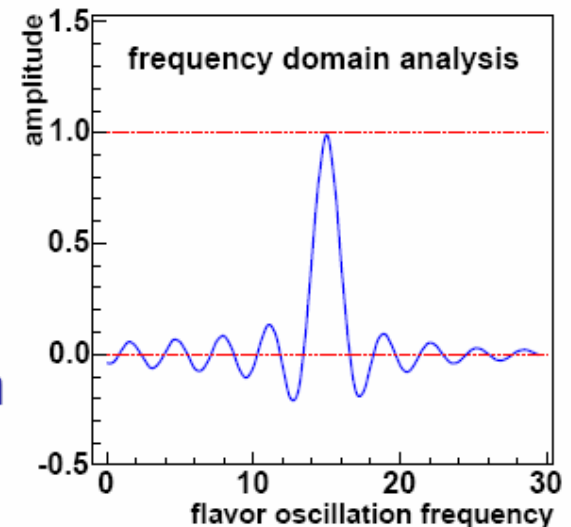
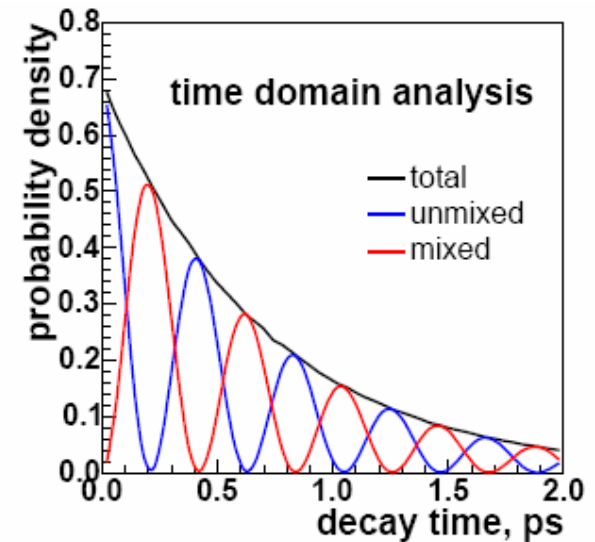
→ fit for  $\mathcal{A}$  at different  $\Delta m_s$

⇒ obtain frequency spectrum

→ **true  $\Delta m_s \Rightarrow \mathcal{A} = 1$ , else  $\mathcal{A} = 0$**

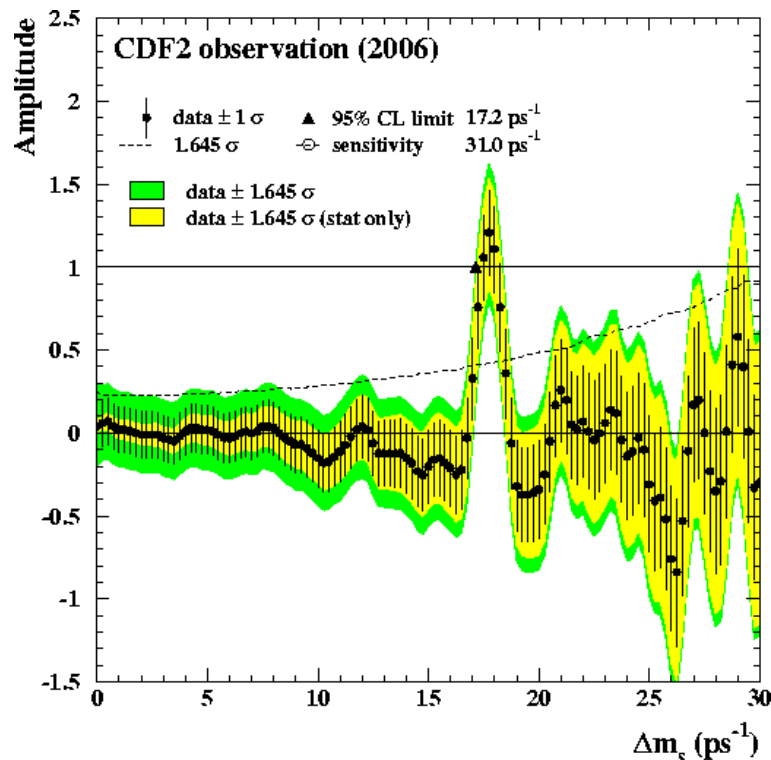
→ traditionally used for  $B_s^0$  mixing search

⇒ easy to combine experiments



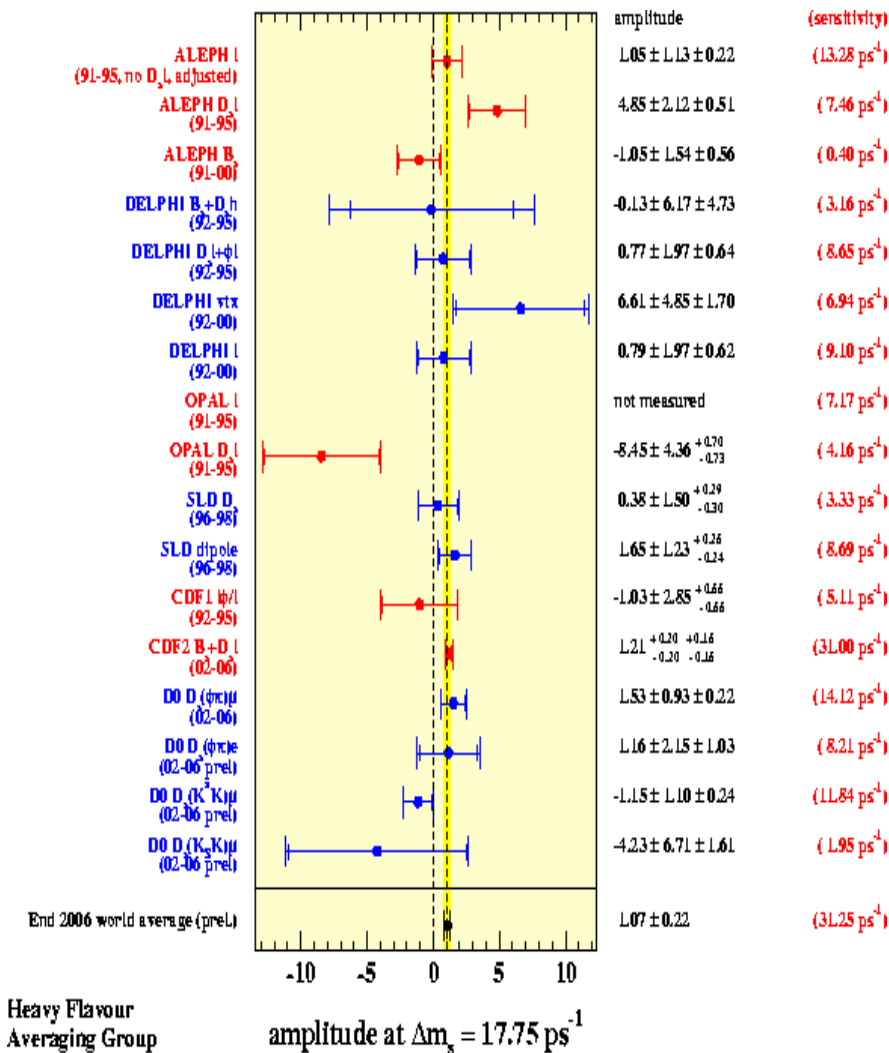
Courtesy of G. Gomes-Ceballos, FPCP 2006, Vancouver, Canada

# $\Delta m_s$ Measurement at the TeVatron: Result



**CDF obtained the first direct evidence of  $\Delta m_s$ !**

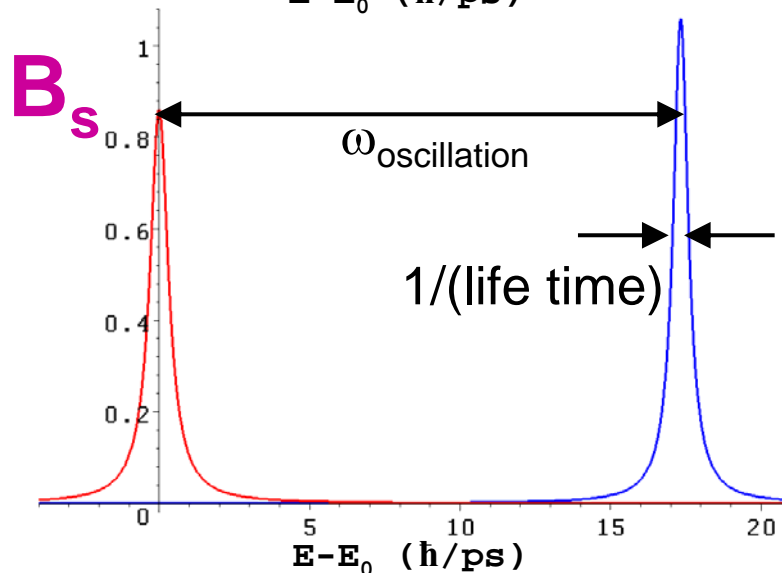
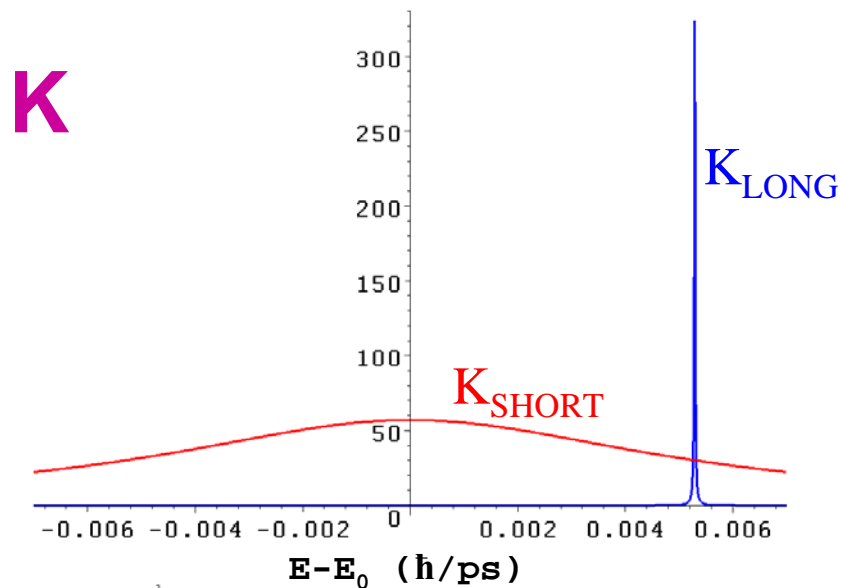
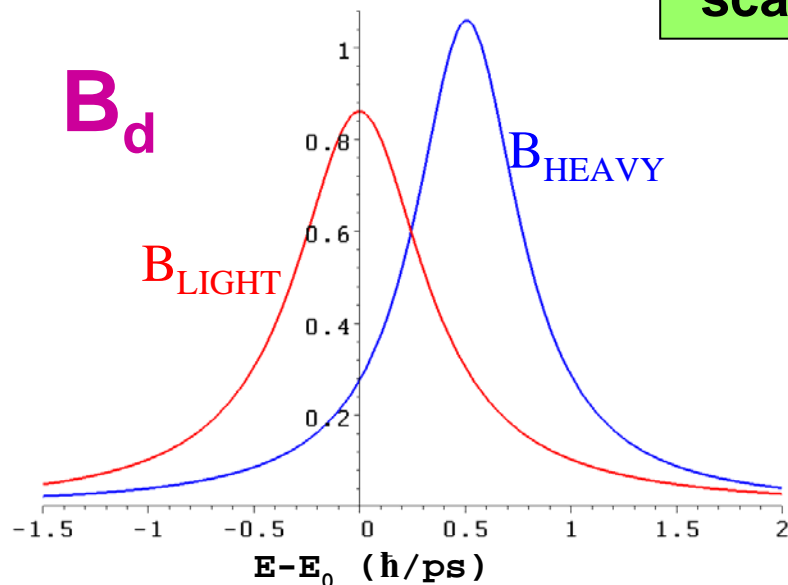
$$\Delta m_s = 17.77 \pm 0.10\text{ (stat)} \pm 0.07\text{ ps}^{-1}$$



# Comparison of $K$ , $B_d$ and $B_s$ Oscillations

- Analogy: coupled Harmonic Oscillator
- Oscillations (mixing) characterized by mass and lifetime differences between the two eigenstates of weak interaction.
- Differences between flavors:
  - $K$ : very different states
  - $B_d$ : Oscillation and decay are comparable
  - $B_s$ : Rapid oscillations

**Mind the scales!**



# D-Oscillations are now Measured

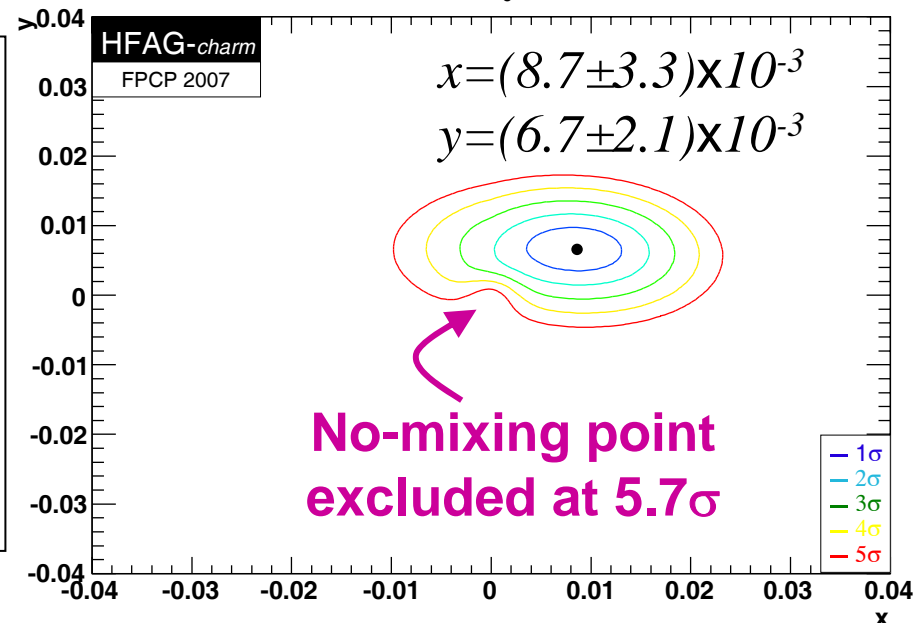
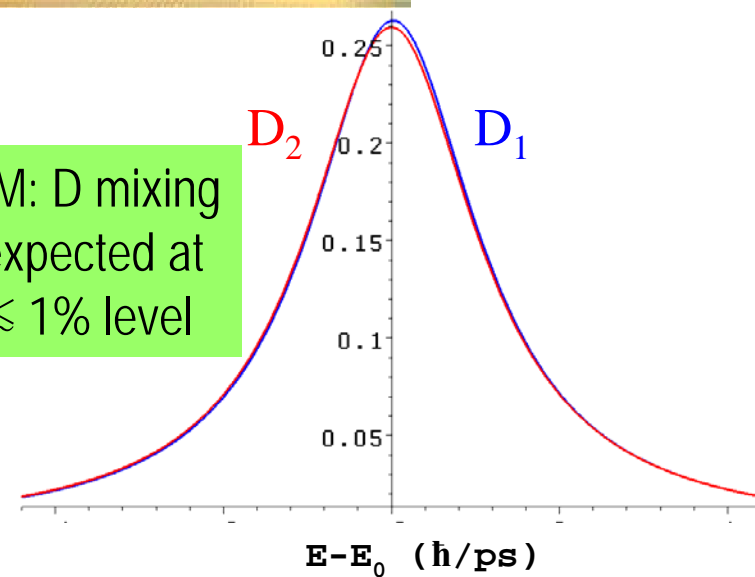
- An experimental challenge!
- Both BaBar and Belle observed mixing (Winter 2007)
- Results are consistent with SM
- Charm: only place where CP violation with down-type quarks in the mixing diagram can be explored.
- No evidence for CP violation
- We need more Measurements with different techniques to get  $x$  and  $y$  parameters.

$$x = \frac{m_1 - m_2}{\Gamma}$$

$$y = \frac{\Gamma_1 - \Gamma_2}{2\Gamma}$$

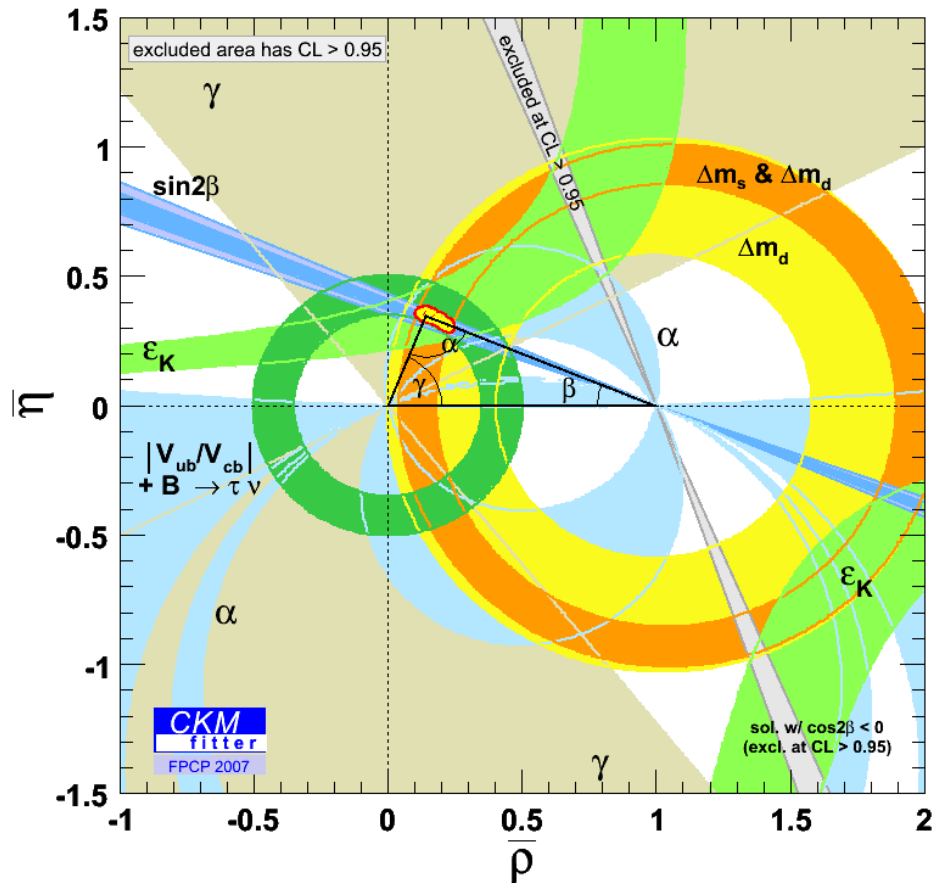
$$\Gamma = \frac{1}{2}(\Gamma_1 + \Gamma_2)$$

SM: D mixing expected at  $\lesssim 1\%$  level



# Summary and Conclusions (I)

## Back to the Unitarity Triangle Fit



CKMfitter Group Eur. Phys. J. C41, 1-131 (2005)

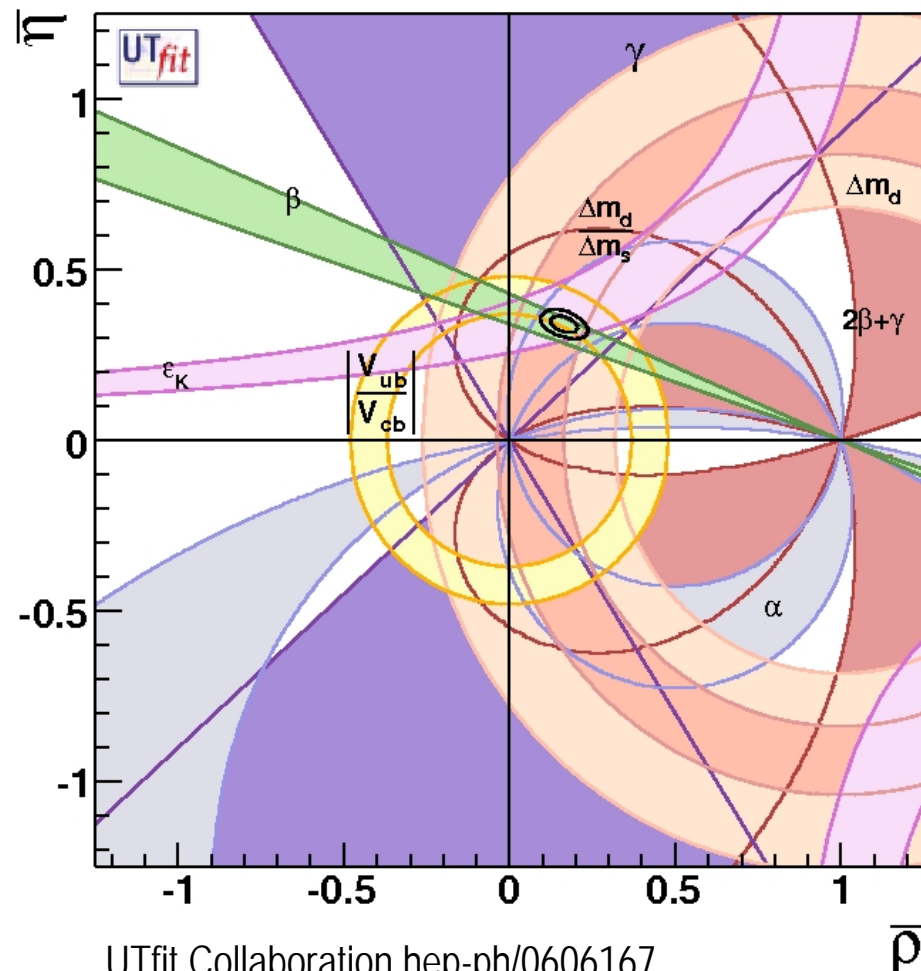
$$\begin{array}{l} \rho = 0.141^{+0.043}_{-0.016} \parallel 0.213^{+0.014}_{-0.024} \\ \eta = 0.311^{+0.015}_{-0.012} \parallel 0.348^{+0.012}_{-0.021} \end{array}$$

- In this talk I have only focused of a few recent results on CP violation
- After many results from B-Factories and measurement of  $\Delta m_s$  by CDF All the independent constraints superimpose in a small region of the  $(\rho, \eta)$  plane!
- Great success of the Standard Model and the CKM Picture



# Summary and Conclusions (II)

## Back to the Unitarity Triangle Fit



$$\rho = 0.164 \pm 0.029$$
$$\eta = 0.340 \pm 0.017$$

There is room for additional effort in the Flavor sector

- There are still small tensions in the fit
- However, if there is physics beyond the Standard Model, the present results constrain it strongly
- Possible New Physics scenarios are likely to have a similar flavor structure similar to the one of the SM (MFV models).
- Eventual New physics should appear as “corrections” to the CKM picture.

**Super-B Factory?**

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I would like to thank Julie Malcles and Achille Stocchi, who authorized me to use materiel which has greatly benefited this talk